

# Importance of Flavour Factories in the LHC Era

new physics search in flavour physics

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RAL, June 1 2005

## Opportunities in Flavour Physics

- Introduction
  - QCD  $\leftrightarrow$  New Physics
  - Interplay of Flavour and Collider Physics
- Exploration of Higher Scales via Rare Decays
  - Inclusive Rare Decays  $\bar{B} \rightarrow X_s \gamma$ ,  $\bar{B} \rightarrow X_s \ell^+ \ell^-$
  - $K \rightarrow \pi \nu \bar{\nu}$
- $B \rightarrow \pi\pi$ ,  $B \rightarrow K\pi$ 
  - QCD Factorization, SCET
  - Nonfactorizable Contributions
- Correlation of Collider and Flavour Physics via Squark Mixing
- CP Violating Observables

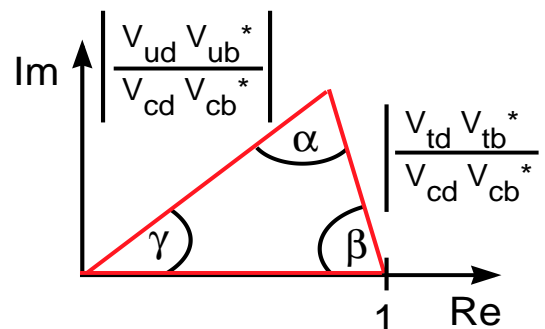
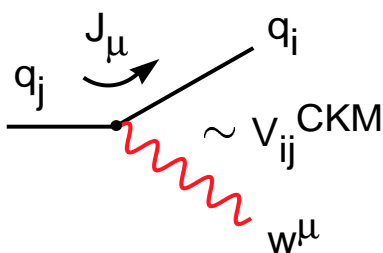
Reviews of Modern Physics 75 (2003) 1159

# Introduction

$$\mathcal{L}_{SM} = \mathcal{L}_{Gauge}(A_i, \psi_i) + \mathcal{L}_{Higgs}(\Phi, \psi_i, v)$$

- **Electroweak precision data** of LEP (CERN), SLC (SLAC), TEVATRON (FERMILAB) confirmed SM predictions within the gauge sector up to a precision of **0.1%**.
- **Scalar Higgs particle**  $\Phi$  not found yet: mechanism of electroweak symmetry breaking is an open issue.
- **Flavour physics**: testing the SM beyond the gauge interactions (differences between fermion families  $\Psi_i$ )

$$\mathcal{L}_{CC} = -\frac{g}{\sqrt{2}} \left[ (\bar{\nu}_e, \bar{\nu}_\mu, \bar{\nu}_\tau) \gamma^\mu \begin{pmatrix} e_L \\ \mu_L \\ \tau_L \end{pmatrix} + (\bar{u}_L, \bar{c}_L, \bar{t}_L) \gamma^\mu V_{CKM} \begin{pmatrix} d_L \\ s_L \\ b_L \end{pmatrix} \right] W_\mu^\dagger$$



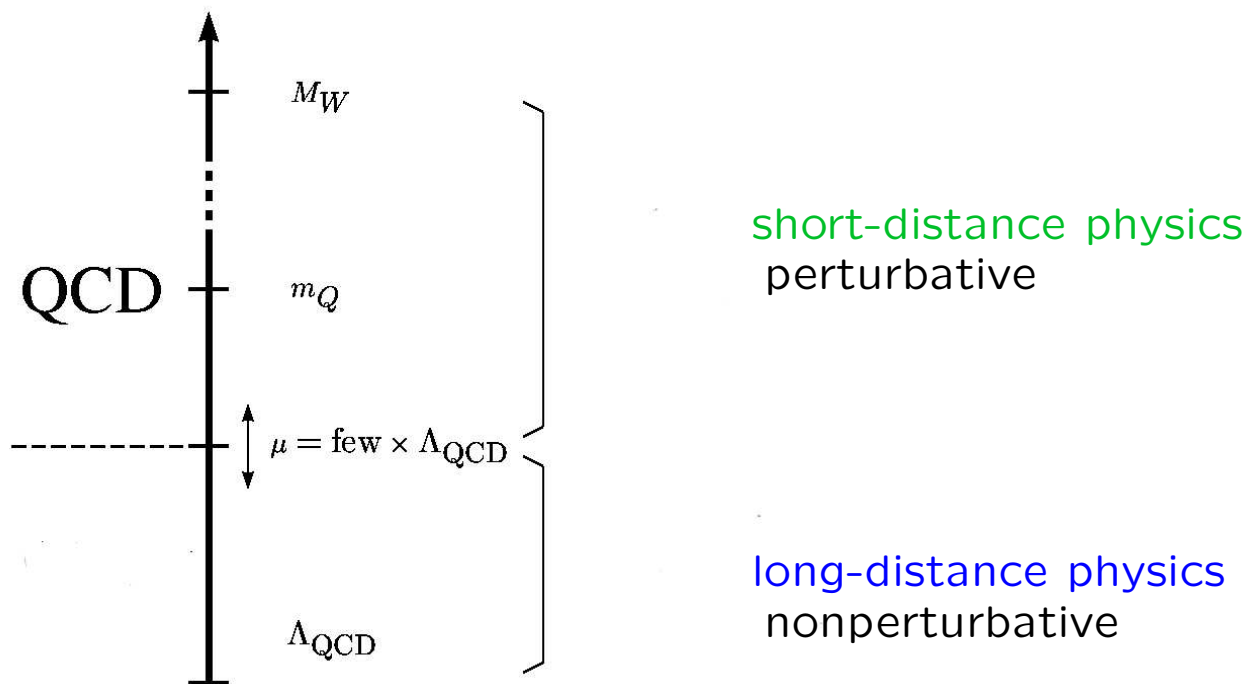
$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

- **Focus:** \* neutrino physics \* B meson physics

- Interplay of LHC and ILC:  
Complementarity of discovery and precision machine  
⇒ LHC/ILC study group
- However: ILC will not be built before 2016 (optimistic!)
- Obvious question:  
What is the role of the flavour factories in this game?
- Experimental 'Roadmap' of flavour physics:
  - $e^+e^-$ - $B$ -experiments:  
 $B$  factories (Babar,Belle)  $\geq$  1999, CLEO III  $\geq$  2000,  
Upgraded  $B$  factories, Super  $B$  factories  $\geq$  2010
  - Hadronic  $B$ -experiments:  
Tevatron II  $\geq$  2001, LHC (Atlas,CMS,LHCb)  $\geq$  2007,  
( $B$ TeV  $\geq$  2009)
  - Kaon-experiments:  
Kopio,BNL ( $K_L \rightarrow \pi^0 \nu \bar{\nu}$ ),  
NA 48/3,CERN ( $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ )  $\geq$  2010
- Interplay of flavour and collider physics
  - Exploration of higher scales via rare decays
  - Correlations between  $B$  and collider physics  
via squark mixing within Susy

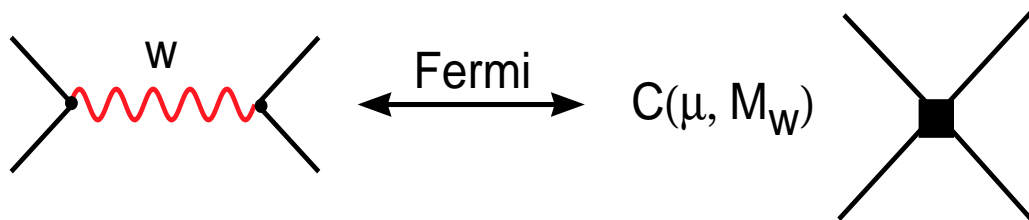
- Main issues of the  $B$  physics program:
  - Mechanism of CP violation in the B system
  - Indirect effects of new physics in rare B decays
  - Studies of strong interactions, QCD, SCET
- New physics:
  - No strict argument that **new** flavour physics must appear at the electroweak scale
  - Baryon asymmetry: one needs more sources of CP violation, not necessarily relevant at low energies .
  - Flavour sector leads to severe constraints for new physics.
  - Flavour structure is a model-dependent issue.
- Decays of  $B$  mesons:
 
$$B_{d,(s)}^0 = \bar{b}d(s), \quad \bar{B}_{d,(s)}^0 = b\bar{d}(\bar{s}), \quad B_u^+ = \bar{b}u, \quad B_u^- = b\bar{u}$$
  - \*  $b$  quark heaviest quark with pronounced hadronic bound states (QCD tests)
  - \* rich CKM phenomenology
  - \* independent test of the mechanism of CP violation ( $\leftrightarrow$  K system)
  - \* interplay of strong and weak interaction
  - $\Rightarrow$  **problem of long-distance strong interactions restricts opportunities in flavour physics significantly**
  - (see hadronic uncertainties in present  $g - 2$  analysis)

Separation of scales necessary !



- **Operator product expansion:**  
Factorization of **short-distance** and **long-distance** physics  
Example: QCD at electroweak scale  $\mu^2 \approx M_W^2$  :  
 $C_i$ : **effective couplings**    $\langle \mathcal{O}_i \rangle$ : **matrix elements**

$$H_{eff} = -\frac{4G_F}{\sqrt{2}} \sum C_i(\mu, M_{heavy}) \mathcal{O}_i(\mu)$$

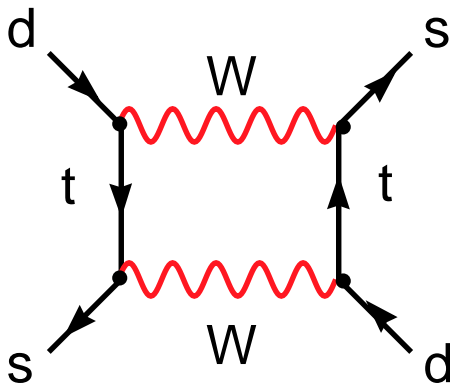


- $\Lambda_{QCD} \ll m_Q = m_b$  :  $1/m_b$  expansion allows for separation of effects  $\mu^2 \approx m_b^2, m_b \Lambda_{QCD}$   
 $\Rightarrow$  **effective theories:** HQET, SCET
- $\mu^2 \approx \Lambda_{QCD}^2$  : long-distance hadronic parameters  
**lattice-QCD**, U-spin symmetry, QCD sum rules, chiral perturbation theory, ...
- $\mu^2 \approx M_{New}^2 \gg M_W^2$  :  
'new physics' effects:  $C_i^{SM}(M_W) + C_i^{New}(M_W)$

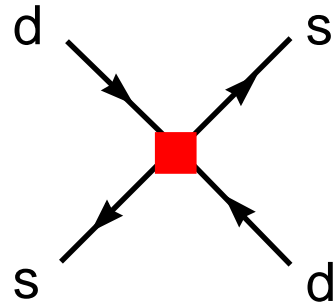
## Exploration of higher scales via flavour observables

$$\mathcal{L} = \mathcal{L}_{Gauge} + \mathcal{L}_{Higgs} + \sum_i \frac{c_i^{New}}{\Lambda} \mathcal{O}_i^{(5)} + \dots$$

- SM as effective theory valid up to cut-off-scale  $\Lambda$
- $K^0 - \bar{K}^0$ -mixing  $\mathcal{O}^6 = (\bar{s}d)^2 \Rightarrow \Lambda > 100 \text{ TeV}$



$$\Rightarrow c^{SM} / M_W^2 \times (\bar{s}d)^2$$

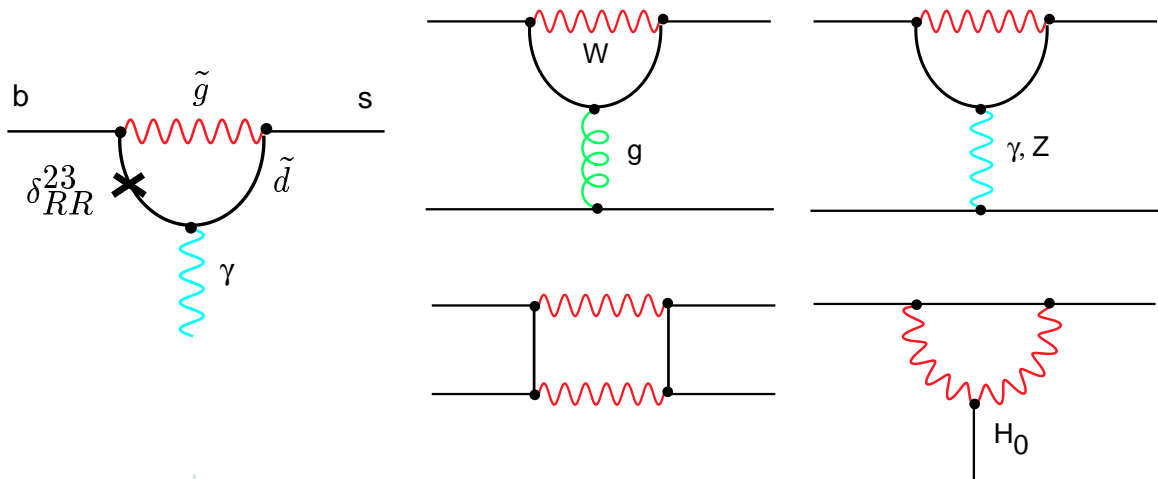


$$c^{New} / \Lambda^2 \times (\bar{s}d)^2$$

- Natural stabilisation of Higgs boson mass  $\Rightarrow \Lambda \sim 1 \text{ TeV}$   
i.e. supersymmetry, superpartner:  $\Lambda_{SUSY} \lesssim 1 \text{ TeV}$   
(but: little hierarchy problem)
- Expectation:  
flavour mixing restricted by additional symmetries  
Rare decays and specific CP violating observables  
allow to analyse flavour symmetry breaking

$$\mathcal{L} = \mathcal{L}_{Gauge} + \mathcal{L}_{Higgs} + \sum_i \frac{c_i^{New}}{\Lambda} \mathcal{O}_i^{(5)} + \dots$$

- Flavourblind elektroweak structure of  $\mathcal{O}_i$  :
  - connects various (theoretically clean !) observables:  
i.e.  $A_{CP}(B_d \rightarrow \Phi K_S) \Leftrightarrow BR(B \rightarrow X_s \gamma)$



- allows for model-independent analysis:

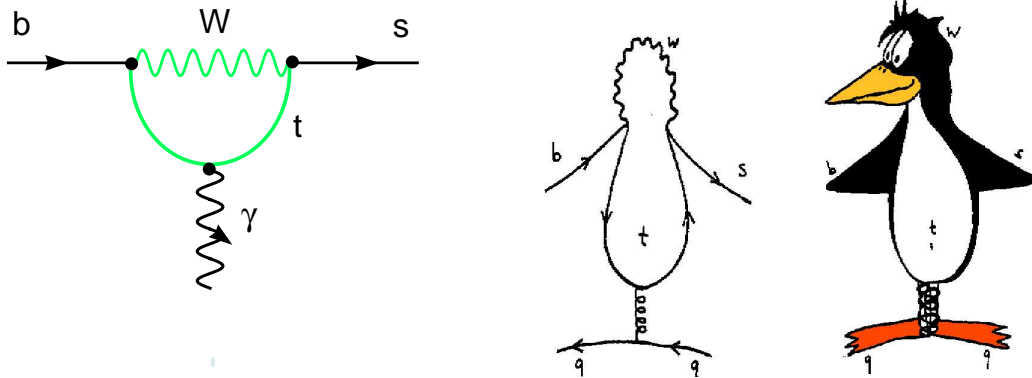
$$BR(B \rightarrow X_s \ell^+ \ell^-), A_{FB}(B \rightarrow X_s \ell^+ \ell^-), A_{CP}(B \rightarrow X_s \gamma),$$

$$BR(B \rightarrow \ell^+ \ell^-), BR(K^+ \rightarrow \pi^+ \nu \bar{\nu}), BR(B \rightarrow X_s \nu \bar{\nu}), \dots$$

- Flavour part of  $\mathcal{O}_i$  :
  - new flavour structures, i.e. squark-mixing in SUSY
  - or
  - minimal flavour violation
    - \* flavour symmetry / CP broken by Yukawa couplings only
    - \*  $[b \rightarrow s] \leftrightarrow [b \rightarrow d] \leftrightarrow [s \rightarrow d]$
    - \* RG-invariant definition (d'Ambrosio et al.)

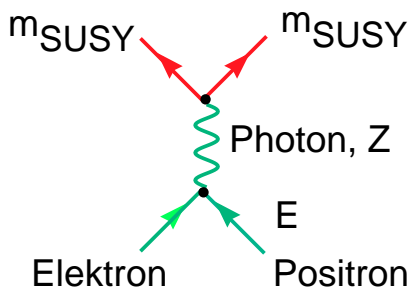


- Rare B decays like  $b \rightarrow s \gamma$  or  $b \rightarrow s l^+ l^-$  directly probe the SM at the one-loop level.



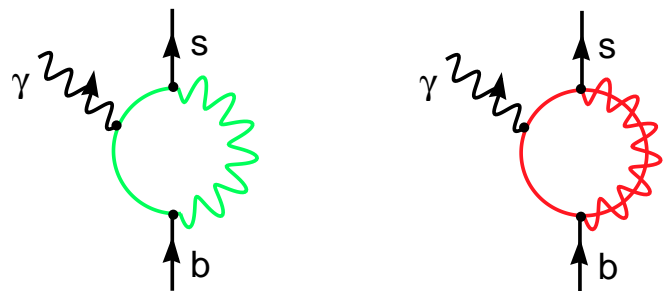
- Search strategies for new degrees of freedom beyond the SM (i.e. for supersymmetry)

Direct:

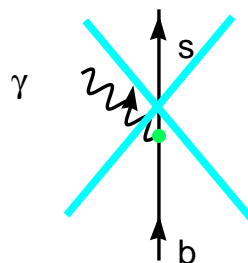


$$2m_{\text{SUSY}}c^2 \leq E$$

Indirect:

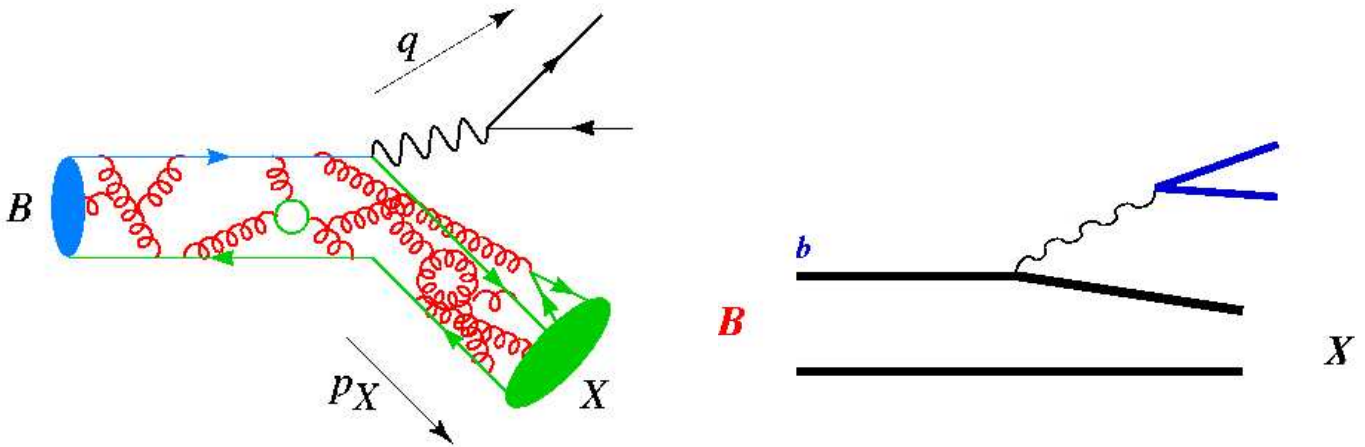


- High sensitivity for 'New Physics', because



$\leftrightarrow$  elektroweak precision data (10%  $\leftrightarrow$  0.1%)

This indirect information is analogous to some direct information a linear collider could provide.



Crucial problem:  
Separation of new physics effects and hadronic uncertainties!

\* focus on inclusive modes:

$$\Gamma(\bar{B} \rightarrow X_s \gamma) \xrightarrow{m_b \rightarrow \infty} \Gamma(b \rightarrow X_s^{\text{parton}} \gamma), \quad \Delta^{\text{nonpert.}} \sim \Lambda_{QCD}^2 / m_b^2$$

No linear term  $\Lambda_{QCD}/m_b$   
Perturbatively calculable contribution dominant

\* focus on ratios of exclusive modes like asymmetries  
(hadronic uncertainties partially cancel out)

\* focus on specific decays like  $B \rightarrow \ell^+ \ell^-$  or  $K \rightarrow \pi \nu \bar{\nu}$   
(hadronic matrix elements known from experiment)

## Perturbative corrections in inclusive decays

- Electroweak two-loop corrections play a subdominant role
- Perturbative QCD corrections are large and lead to  $\alpha_s(M_W) \text{Log}(m_b^2 / M_W^2) \rightarrow$  resummation of Logs necessary:

LL      Leading Logs                       $G_F (\alpha_s \text{Log})^N$                $N = 0, 1, ..$

NLL    Next-to-Leading Logs     $G_F \alpha_s (\alpha_s \text{Log})^N$

- Effective field theory ( $\mu \approx M_W$ )

$$H_{eff}(b \rightarrow sl^+\ell^-) = -\frac{4G_F}{\sqrt{2}} V_{bt}V_{st}^* \sum_{i=1}^{10} C_i(\mu) \mathcal{O}_i(\mu)$$

$$C_i(\mu) \langle \text{Diagram} \rangle + C_7(\mu) \langle \text{Diagram with } \gamma \rangle + C_8(\mu) \langle \text{Diagram with } g \rangle$$

$\mathcal{O}_i(\mu)$                        $\mathcal{O}_7(\mu)$                        $\mathcal{O}_8(\mu)$

$$+ C_9(\mu) \langle \text{Diagram with } e^+e^- \rangle + C_{10}(\mu) \langle \text{Diagram with } e^+e^- \rangle$$

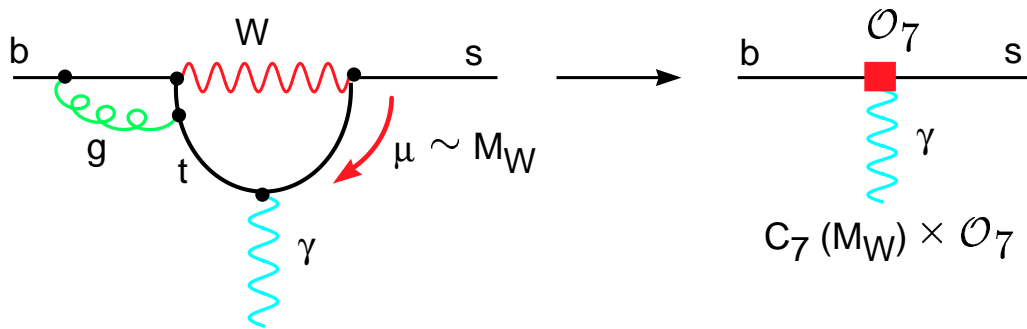
$\mathcal{O}_9(\mu)$                        $\mathcal{O}_{10}(\mu)$

$C_i$ : dynamical information on physics  $\mu > M_W$

$\mathcal{O}_i$ : effective dynamics (5 quarks und  $\gamma, gluon$ )  $\mu < M_W$

\* Initial conditions  $C_i(\mu \simeq M_W)$   
 (Adel, Yao) (Greub, Hurth)

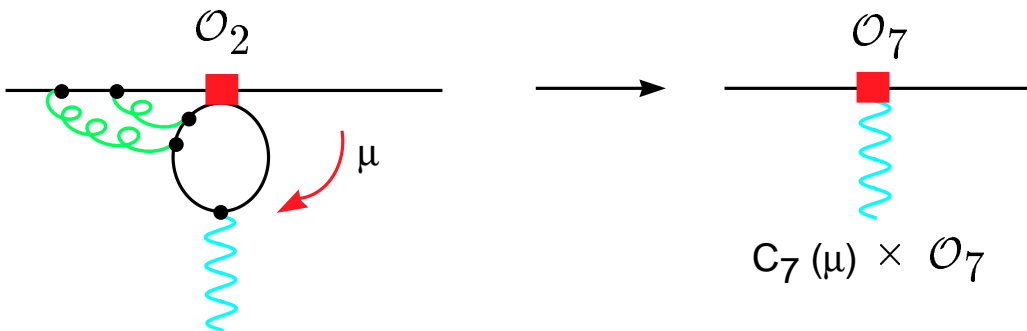
\* sensitivity for 'new physics' \* no large logs



\* Coefficients  $\gamma_{ij}$  in  $\mu \frac{d}{d\mu} C_i(\mu) = \gamma_{ij} C_j(\mu) \Rightarrow C_i(\mu \simeq m_b)$   
 (Chetyrkin, Misiak, Münz) (Gambino, Gorbahn, Haisch)

QCD-mixing of operators:

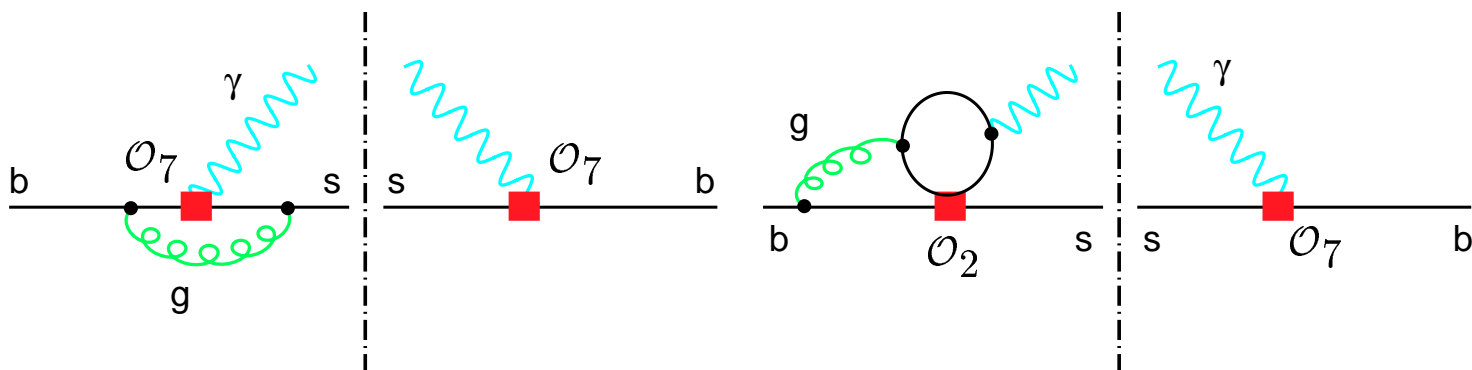
'new physics' information in  $C_7(M_W)$  gets covered up



\* Matrix elements  $\langle O_i(\mu \simeq m_b) \rangle$   
 (Greub, Hurth, Wyler) (Buras et al.)

\* perturbative contributions are dominant

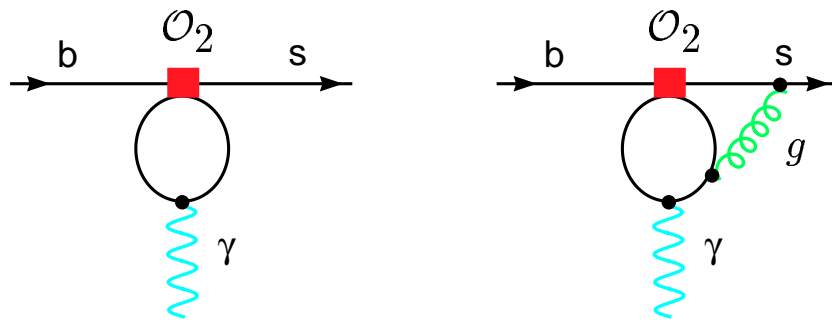
\*  $\Gamma(B \rightarrow X) \sim Im \langle B | H_{eff} H_{eff} | B \rangle$



\* two-loop diagrams of operator  $\mathcal{O}_2$

## Present status of $\bar{B} \rightarrow X_s \gamma$

Problem: renormalization scheme of the charm mass (NNLL)



$$m_c^{\text{pole}}/m_b^{\text{pole}} = 0.29 \pm 0.02 \Leftrightarrow m_c^{\overline{\text{MS}}}(\mu)/m_b^{1\text{S}} = 0.23 \pm 0.05$$

$\Rightarrow$  central value  $\sim +11\%$  (Gambino, Misiak)

Our experience  $\overline{\text{MS}}$ -scheme favored  $\Rightarrow m_c/m_b = 0.23_{-0.05}^{+0.08}$

Present NLL Prediction: (Hurth, Lunghi, Porod)

$$BR(\bar{B} \rightarrow X_s \gamma) \times 10^4 = (3.79_{-0.44}^{+0.26} \Big|_{m_c/m_b} \pm 0.02_{\text{CKM}} \pm 0.25_{\text{param}} \pm 0.15_{\text{scale}})$$

NNLL QCD calculation needed for uncertainty  $\ll 10\%$  !  
(work in progress !)

Experiment:

$$BR(\bar{B} \rightarrow X_s \gamma) = (3.52 \pm 0.30) \times 10^{-4}$$

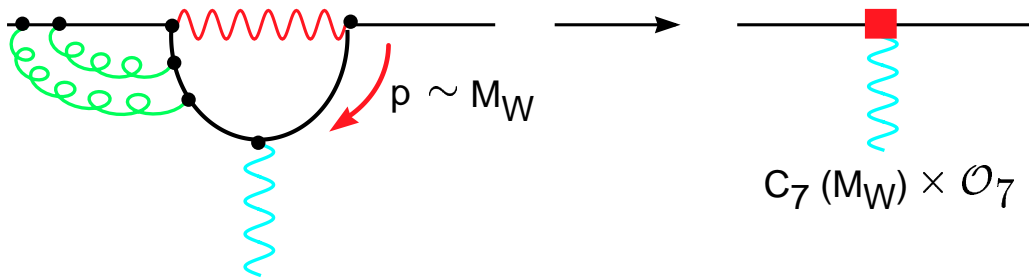
CLEO, ALEPH, BELLE, BABAR

The  $\bar{B} \rightarrow X_s \gamma$  data already leads to significant restrictions on the parameter space of various extensions of the SM.

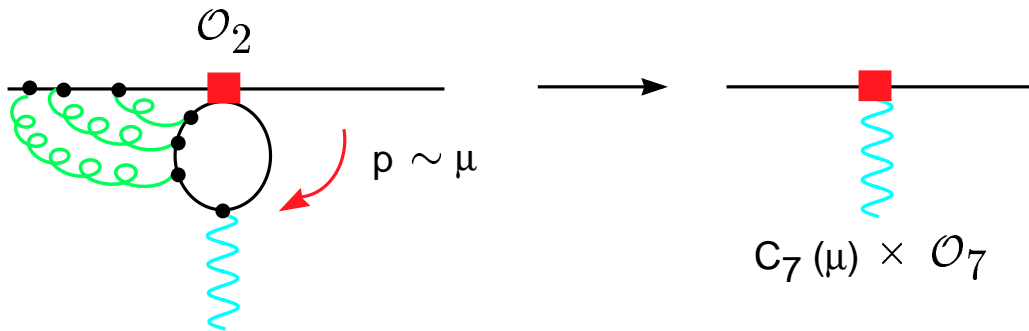
Clearly, this indirect information will be most valuable when the general nature of new physics will be identified in the direct search (LHC).

# NNLL-QCD — work in progress

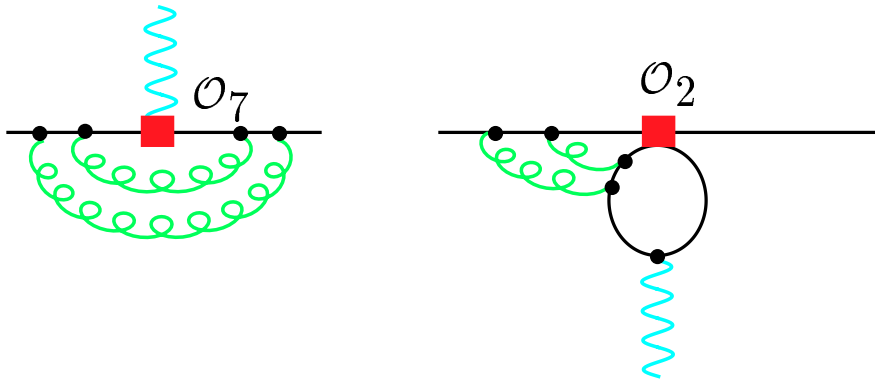
- Initial conditions  $C_i(\mu \simeq M_W)$  **DONE!!** Misiak, Steinhauser



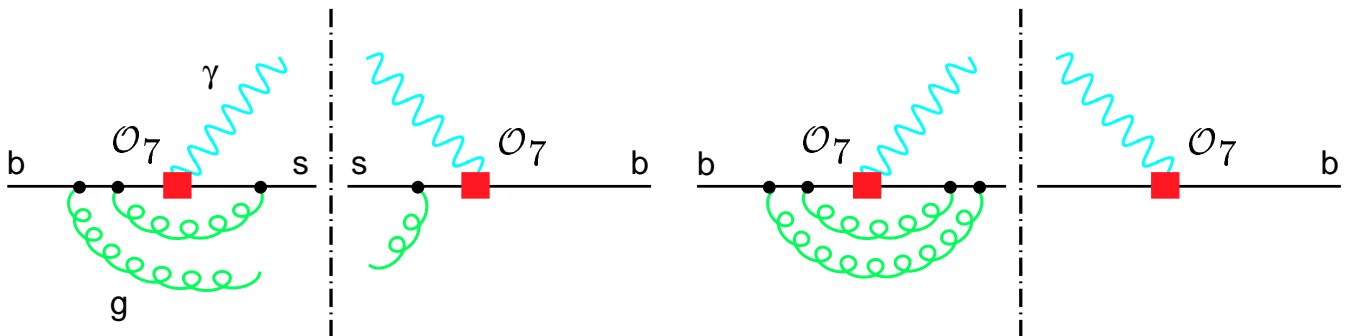
- Coefficients  $\gamma_{ij}$  in  $\mu \frac{d}{d\mu} C_i(\mu) = \gamma_{ij} C_j(\mu) \Rightarrow C_i(\mu \simeq m_b)$



- Matrix elements:  $\langle O_7(\mu \simeq m_b) \rangle$  and  $\langle O_2(\mu \simeq m_b) \rangle$

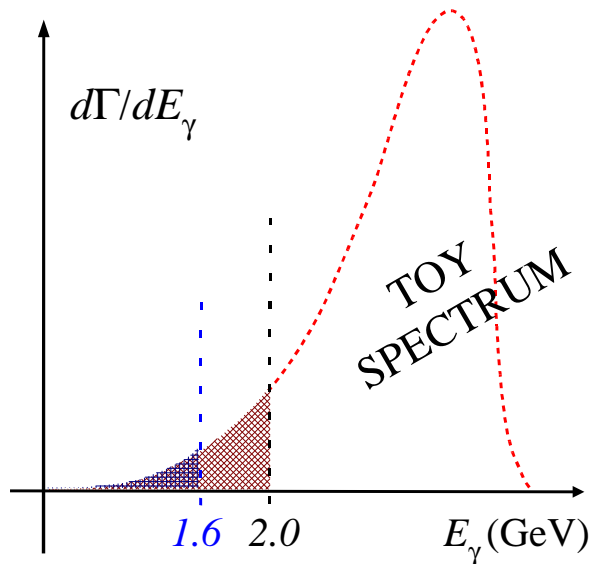


- $\langle O_7(\mu \simeq m_b) \rangle$  Asatrian, Greub, Hurth



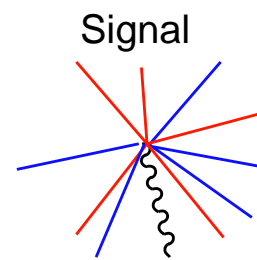
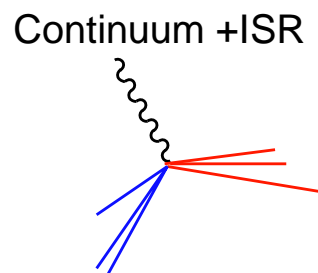
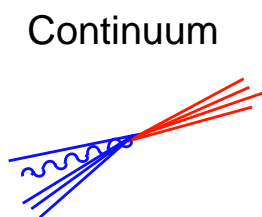
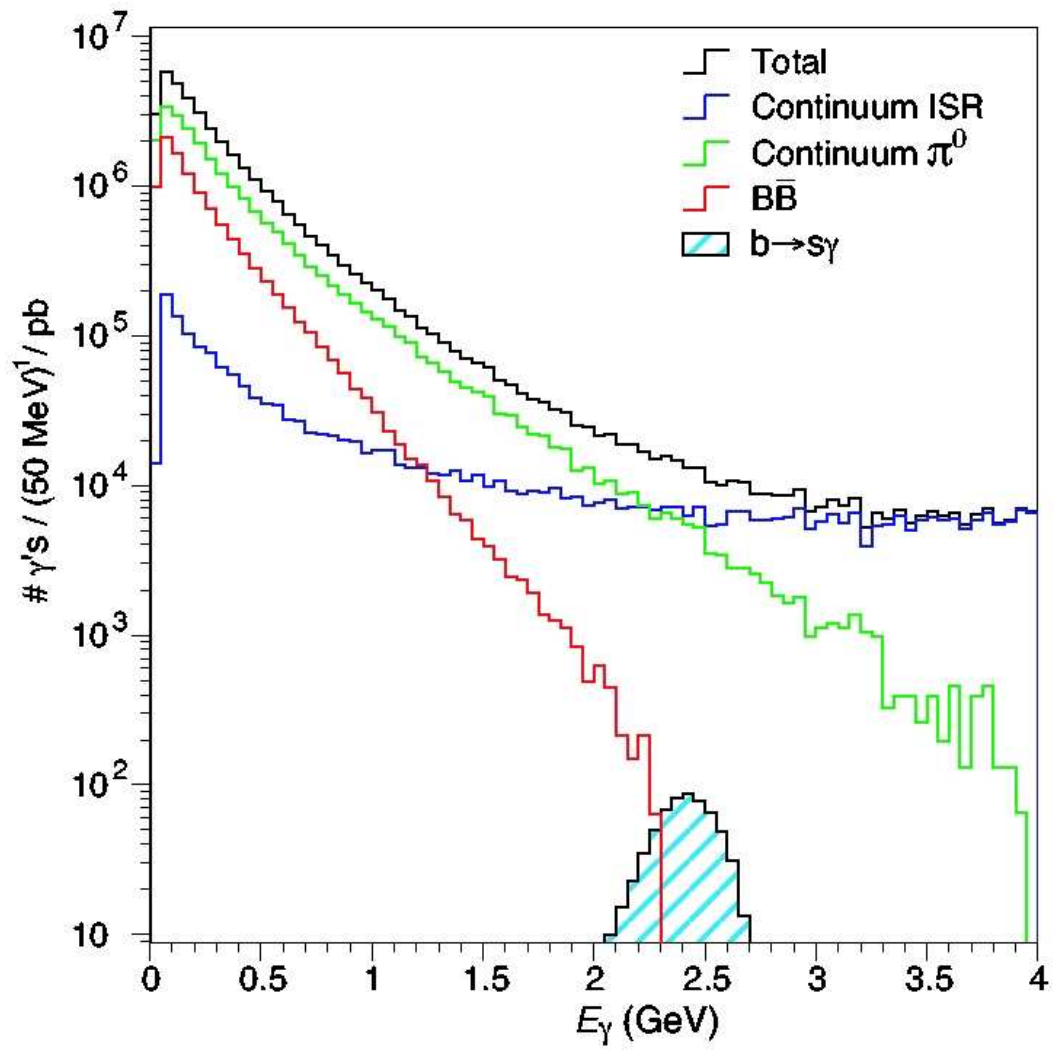
Estimate of the reduction of the scheme dependence at NNLL:  
 Asatrian et al. hep-ph/0505068 12.4%  $\rightarrow$  5.1%

## Experimental issues



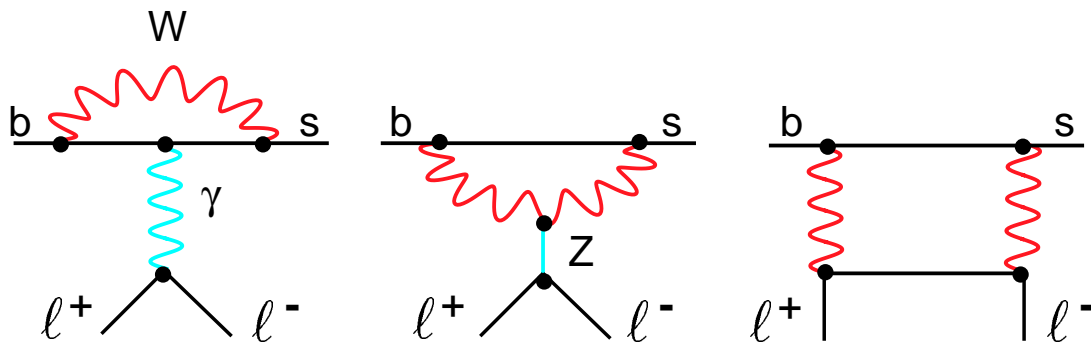
- \* Extrapolation necessary (systematic uncertainty )
- \* Latest Belle measurement (2004): [Cut at 1.8GeV](#)
- \* **Shape of photon spectrum not sensitive for new physics !**

# CLEO





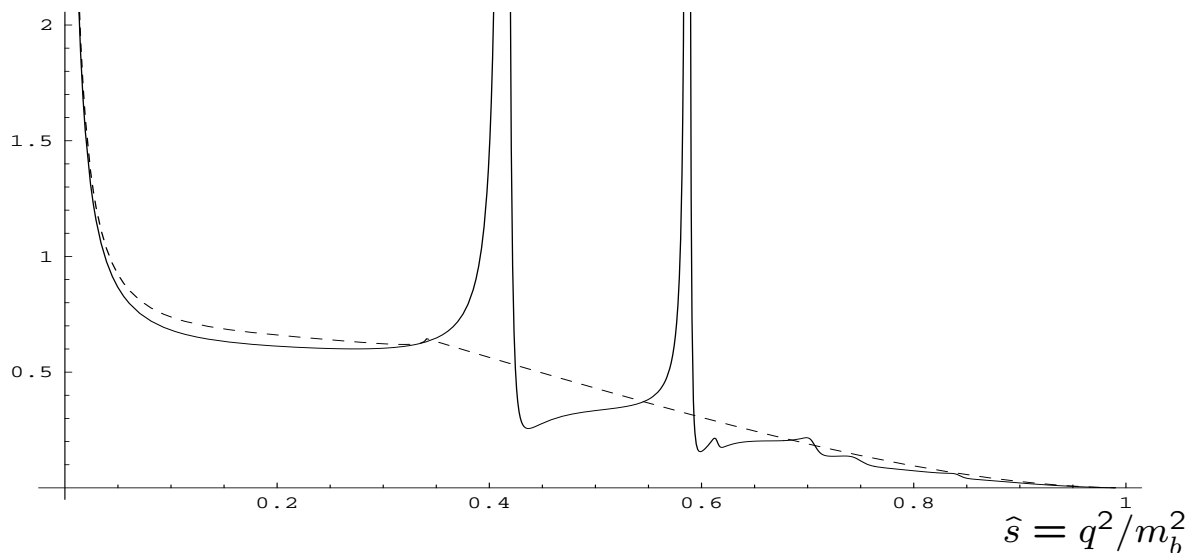
## $\bar{B} \rightarrow X_s l^+ l^-$ : Dilepton mass spectrum



- on-shell- $c\bar{c}$ -resonances

cuts:  $1\text{GeV}^2 < q^2 < 6\text{GeV}^2$  und  $14.4\text{GeV}^2 < q^2$  :  
perturbative contributions dominant

$$\frac{d}{ds} BR(\bar{B} \rightarrow X_s l^+ l^-) \times 10^{-5}$$



- Theory NNLL QCD: Ghinculov, Hurth, Isidori, Yao

$$BR(\bar{B} \rightarrow X_s l^+ l^-)_{\text{Cut: } q^2 \in [1\text{GeV}^2, 6\text{GeV}^2]} = (1.63 \pm 0.20) \times 10^{-6}$$

$$BR(\bar{B} \rightarrow X_s l^+ l^-)_{\text{Cut: } q^2 > 14.4\text{GeV}^2} = (4.04 \pm 0.78) \times 10^{-7}$$

NNLL QCD corrections  $q^2 \in [1\text{GeV}^2, 6\text{GeV}^2]$

central value:  $-14\%$ , perturbative error:  $13\% \rightarrow 6.5\%$

## Experimental issues

- Semi-Inclusive Measurements ( $m(\ell^+\ell^-) > 0.2\text{GeV}$ )

Belle, PRL 90 (2003) 021801 :

$$BR(\bar{B} \rightarrow X_s \ell^+ \ell^-) = (6.1 \pm 1.4(\text{stat}) + 1.4 - 1.1(\text{syst}))10^{-6}$$

Update ICHEP 2004:

$$BR(\bar{B} \rightarrow X_s \ell^+ \ell^-) = (4.11 \pm 0.83(\text{stat}) + 0.74 - 0.70(\text{syst}))10^{-6}$$

Babar, PRL 93 (2004) 081802 :

$$BR(\bar{B} \rightarrow X_s \ell^+ \ell^-) = (5.6 \pm 1.5(\text{stat}) \pm 0.6(\text{syst}) \pm 1.1(\text{mod}))10^{-6}$$

– in agreement with corresponding SM prediction:

$$(4.6 \pm 0.8) \times 10^{-6} \text{ (Ghinculov, Hurth, Isidori, Yao)}$$

not sensitive yet for NNLL

– semiinclusive: modelling of hadronic mass distribution

- Separate experimental data on two perturbative windows in dilepton mass spectrum desirable (Babar already made first separate measurements with large errors)
- End of Babar and Belle (1/ab): 15% accuracy possible
- LHCb: only semi-inclusive analysis possible without the  $\pi_0$  modes
- Fully inclusive measurement possible within a Super- $B$  factory

## $\bar{B} \rightarrow X_s l^+ l^-$ : Forward-backward-charge-asymmetry

$$A_{FB} \equiv \frac{1}{\Gamma_{semilep}} \left( \int_0^1 d(\cos \theta) \frac{d^2\Gamma}{dq^2 d\cos \theta} - \int_{-1}^0 d(\cos \theta) \frac{d^2\Gamma}{dq^2 d\cos \theta} \right)$$

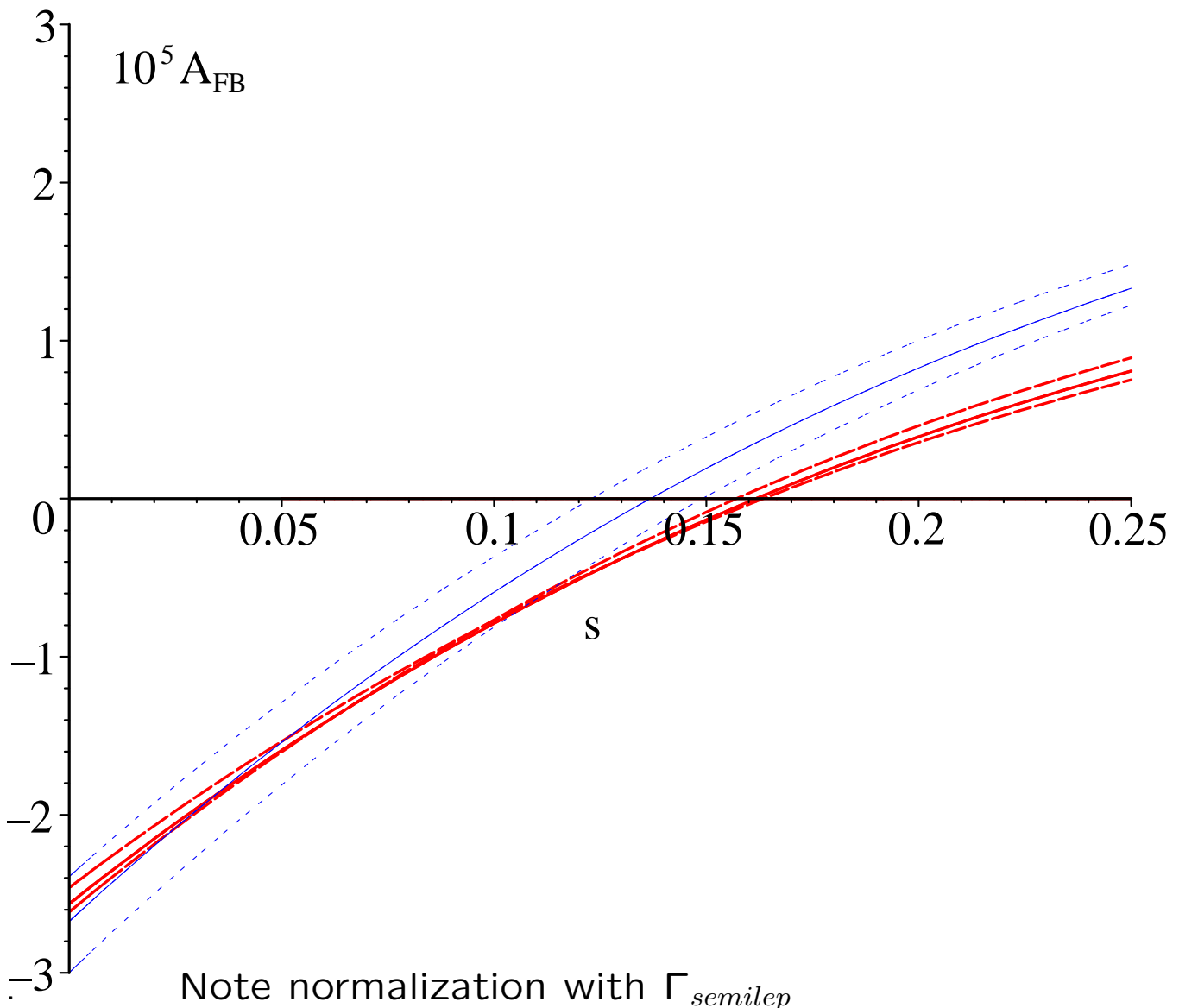
( $\theta$  angle between  $l^+$  and  $B$  momenta in dilepton CMS)

$$A_{FB}(q_0^2) = 0 \quad \text{for} \quad q_0^2 \sim C_7/C_9$$

NNLL corrections induce large  $\sim 16\%$  Shift of the Zero

$$q_0^2 = (3.90 \pm 0.25) GeV^2 \quad \text{Precision test of SM !}$$

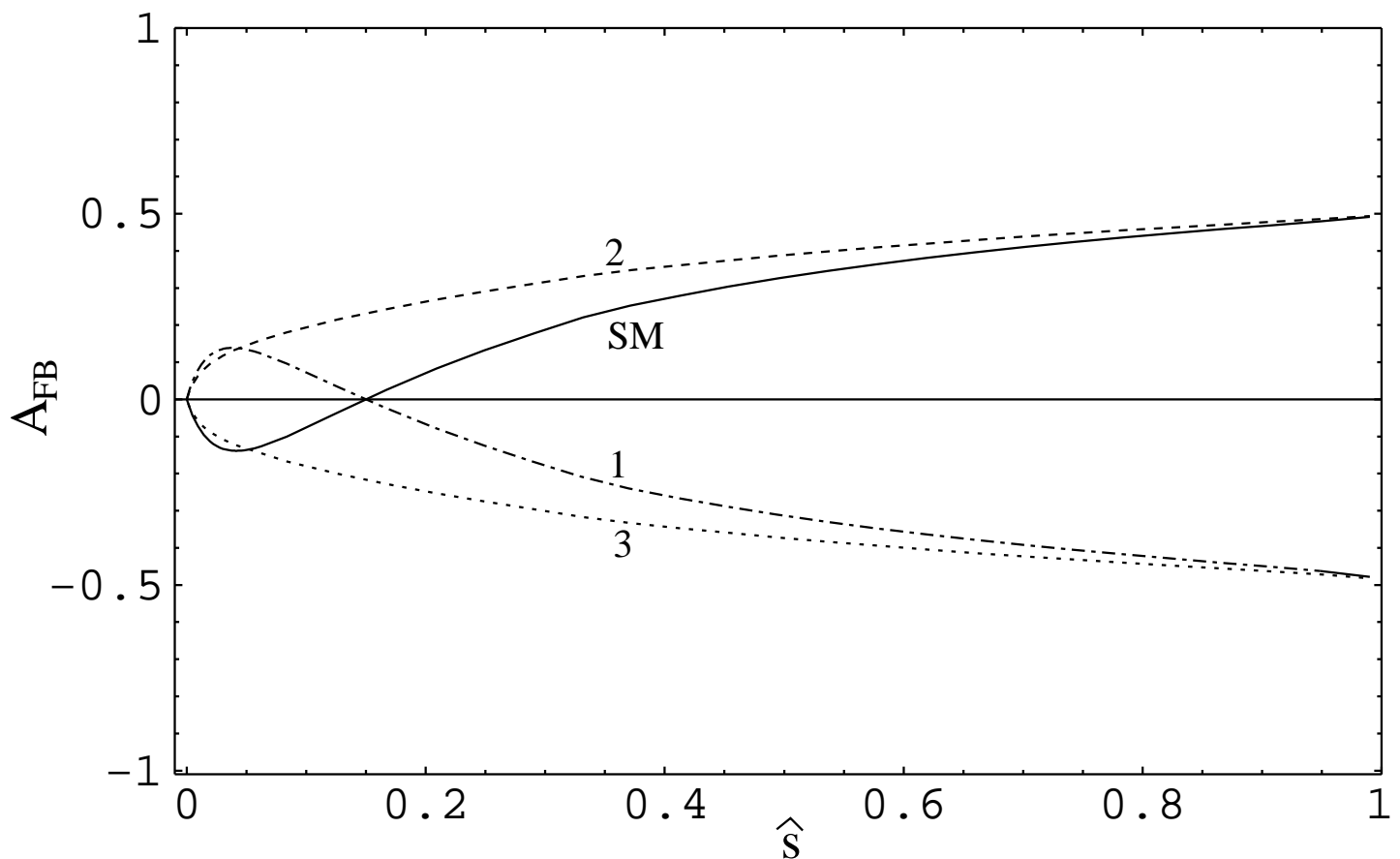
Ghinculov, Hurth, Isidori, Yao  
Asatrian, Bieri, Greub, Hovhannisyan



## New physics search

Four different shapes of the 'normalized' FB asymmetry  $\overline{A}_{FB}$  for the decay  $\overline{B} \rightarrow X_s l^+ l^-$  within the MSSM compatible with the present data.

Hiller et al.



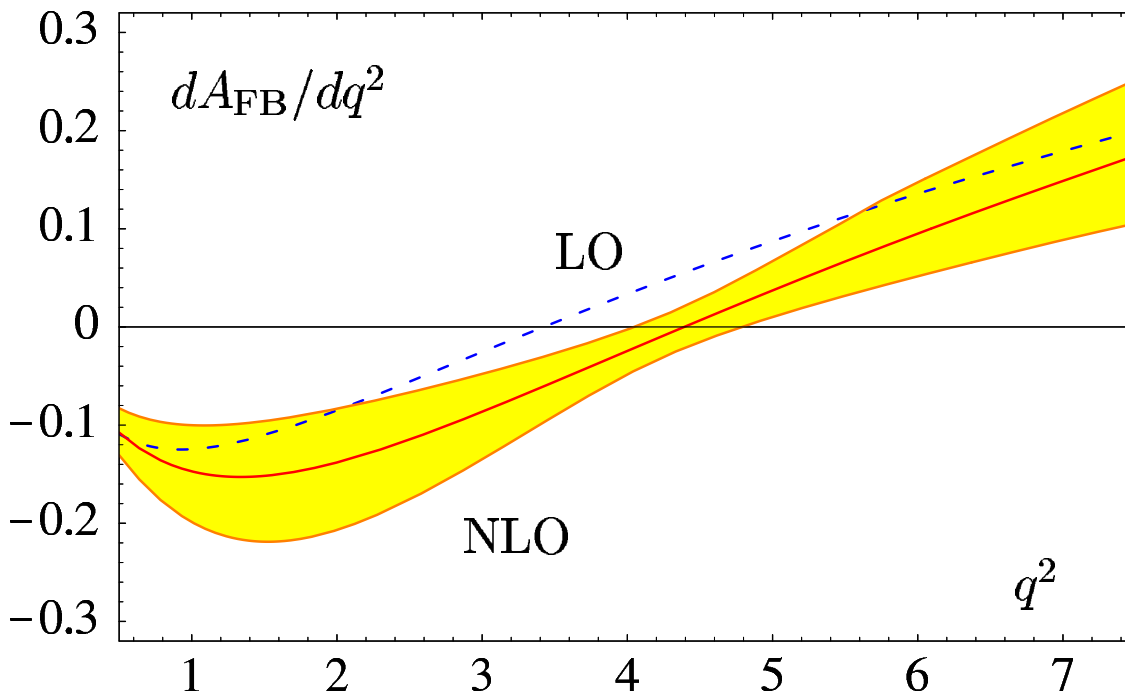
Already a rough measurement of the shape could lead to a signal for new physics !

$$A_{FB} \sim \text{Re}[C_{10}^*(s)C_9^{eff}(s) + f(s)C_7^{eff}(s)]$$

**SM:** large  $q^2$ :  $\mathcal{O}_9(+vector) \times \mathcal{O}_{10}(axialvector)$   
small  $q^2$ :  $\mathcal{O}_7(-vector) \times \mathcal{O}_{10}(axialvector)$

## FB-charge-asymmetry in $B \rightarrow K^* \ell^+ \ell^-$

Beneke, Feldmann, Seidel



- In contrast to the branching ratio the zero of the FBA is almost insensitive to hadronic uncertainties. At LO the zero depends on the short-distance Wilson coefficients only:

$$q_0^2 = q_0^2(C_7, C_9), \quad q_0^2 = (3.4 + 0.6 - 0.5) \text{GeV}^2 \quad (LO)$$

- NLO contribution calculated within QCD factorization approach leads to a large shift:

$$q_0^2 = (4.39 + 0.38 - 0.35) \text{GeV}^2 \quad (NLO)$$

- Issue of power corrections ( $1/m_b$ ) !
- Theoretical errors in branching ratio Ball et al. :

$$\Delta BR(B \rightarrow K^* \mu^+ \mu^-) = (+26, \pm 6, +6, -0.7, \pm 2)\%$$

## conclusions on inclusive rare $B$ decays

- Model-independent analysis of  $b \rightarrow sl^+\ell^-$  and  $b \rightarrow s\gamma$

Global fit to the Wilson coefficients  $C_7, C_9, C_{10}$

–  $\Gamma(B \rightarrow X_s\gamma)$

–  $d\Gamma(B \rightarrow X_s\ell^+\ell^-) / d\hat{s}$

Invariant dilepton mass distribution

–  $A(s) = \int_{-1}^1 d\cos\theta d^2\Gamma(B \rightarrow X_s\ell^+\ell^-) / dsd\cos\theta \operatorname{sgn}(\cos\theta)$

Forward-Backward Charge Asymmetry

$\Rightarrow$  Determines magnitude + sign of  $C_7, C_9, C_{10}$

In MFV the sign of  $C_7$  is already fixed by  $b \rightarrow sl^+\ell^-$  data  
Gambino, Haisch, Misiak

- For new physics search measurements of kinematical distributions are needed (high statistics necessary !):  
Super-B: 7% accuracy in  $s_0$  possible
- Impact of NNLL (NLL) QCD calculations crucial !

Super-B reports

of KEK, hep-ph/0406071, and of SLAC, hep-ph/0503261.

## Future role of kaon physics: Kopio, NA48/3

- BNL–E787: three events 3/2004 !

$$BR(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = \left(1.47 \begin{array}{c} + 1.3 \\ - 0.9 \end{array}\right) \times 10^{-10}$$

- Present SM theory (in future error **below 5%** possible):

$$BR(K^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{SM}} = (0.80 \pm 0.11) \times 10^{-10} .$$

What makes the neutrino modes  $K \rightarrow \pi \nu \bar{\nu}$  so attractive?

- leading hadronic matrix element is known from  $K_{l3}$  decays:  $\langle \pi | (\bar{s}d)_{V-A} | K \rangle$
- amplitude dominated by short-distance due to quadratic GIM:  $A^q \sim m_q^2 V_{qs} V_{qd}$

Neutrino modes as theoretically clean as inclusive  $B$  decays !

⇒ highly sensitive probe for degrees of freedom at higher scales

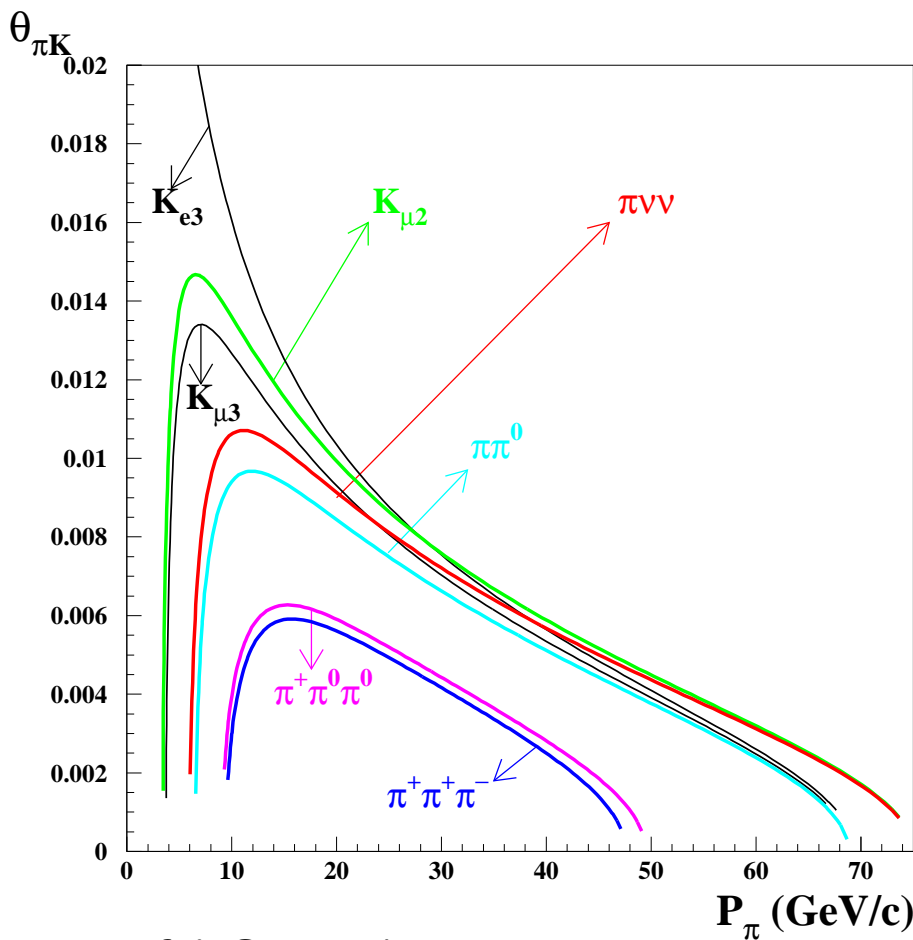
Proposed experiment at CERN, NA48/3: 'decay in flight'

80  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  events in about two years of data taking

( $4 \times 10^{12}$  kaon decays/SPS year, 10% acceptance, SM)

main background:  $K^+ \rightarrow \pi^+ \pi^0$

( $\gamma$  veto much easier because of high energy kaon beam)



courtesy of A.Ceccucci

$P_K = 75 \text{ GeV}/c$



- BNL-E787: 2 events !

$$BR(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = \left( 1.57 \begin{array}{c} + \\ - \end{array} \begin{array}{c} 1.75 \\ 0.82 \end{array} \right) \times 10^{-10}$$

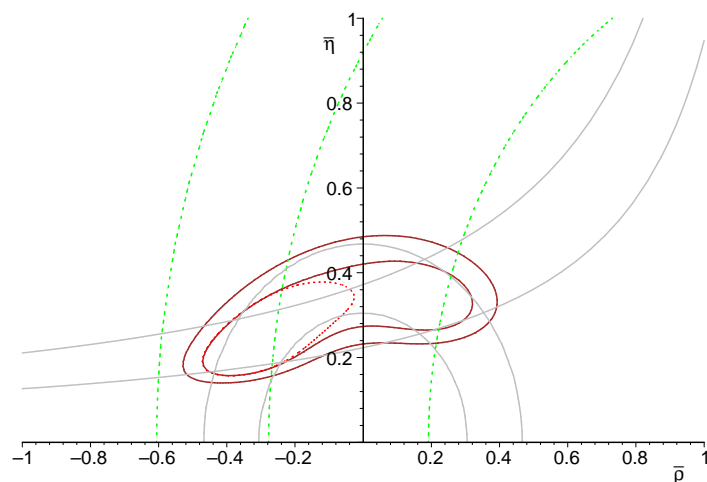
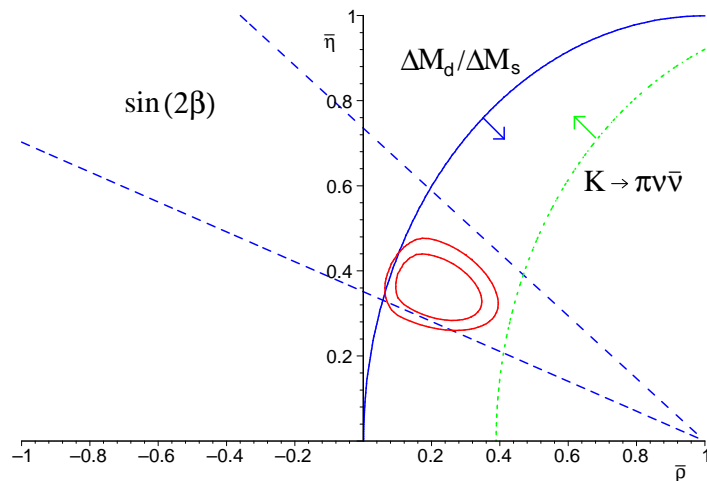
- BNL-E787: Third event 3/2004 !

$$BR(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = \left( 1.47 \begin{array}{c} + \\ - \end{array} \begin{array}{c} 1.3 \\ 0.9 \end{array} \right) \times 10^{-10}$$

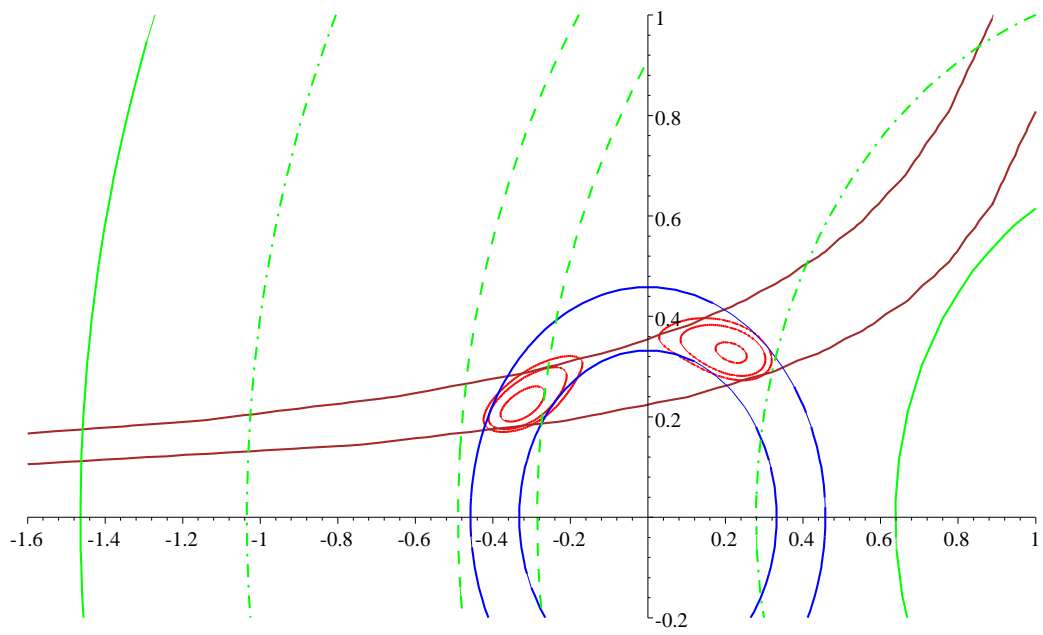
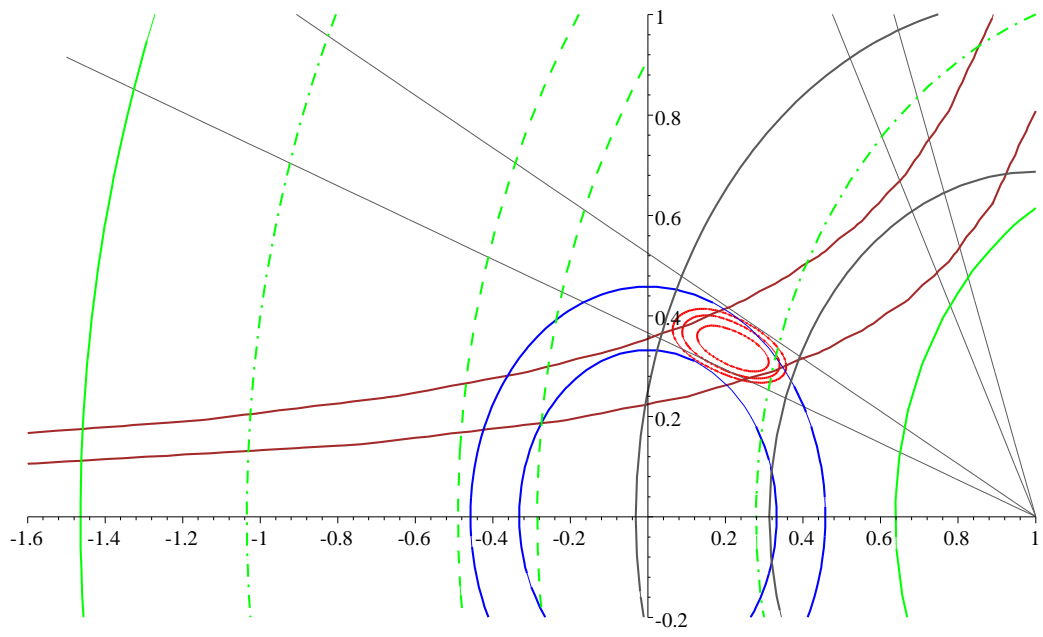
- SM Theory:

$$BR(K^+ \rightarrow \pi^+ \nu \bar{\nu})_{SM} = (0.72 \pm 0.21) \times 10^{-10} .$$

D'Ambrosio, Isidori: some speculation

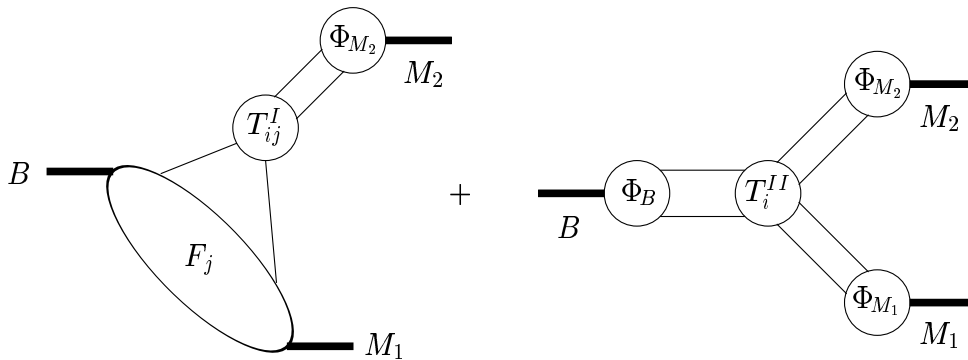


Update after third event (D'Ambrosio, Isidori)



## Hadronic charmless $B$ decays

- QCD factorization theorems for  $B \rightarrow \pi\pi$  and  $B \rightarrow K\pi$



$$\begin{aligned}
 \langle \pi K | Q_i | B \rangle &= F_0^{B \rightarrow \pi} T_{K,i}^I * f_K \Phi_K + F_0^{B \rightarrow K} T_{\pi,i}^I * f_\pi \Phi_\pi \\
 &+ T_i^{II} * f_B \Phi_B * f_K \Phi_K * f_\pi \Phi_\pi, \\
 &+ \text{terms suppressed by } 1/m_b
 \end{aligned}$$

- Factorization in  $B$ -decays
  - Short-distance effects are identified and can be systematically calculated in perturbation theory
  - Non-perturbative effects parametrized in terms of a few universal functions (parton distributions, form factors, light-cone distribution amplitudes)
  - Hope to achieve necessary accuracy to extract CKM elements
  - Limiting factor:**  
Insufficient information on power-suppressed terms  
Challenge for nonperturbative methods !
- Quantum field theoretical description: SCET (no OPE !)  
HQET is not applicable to  $B$  decays in which some of the outgoing, light particles have momenta of order  $m_b$ .

## Phenomenological approach to $B \rightarrow \pi\pi$

Feldmann, Hurth

- Use pure QCD-factorization part ( $\neq$  BBNS) + general isospin analysis of the nonfactorizable part.
- Infer information on nonfactorizable parameters from experimental data by producing random parameters values and calculating the  $\chi^2$ -value

$$A_i(I, \Delta I) = A_i^F(I, \Delta I) + A_i^{NF}(I, \Delta I)$$

$$A_i^{NF}(I, \Delta I) := r_i(I, \Delta I) e^{i\phi_i(I, \Delta I)} A_{\pi\pi}$$

- Nonfactorizable corrections are numerically not negligible  
Default scenario in the BBNS approach where all parameters  $r_i(I, \Delta I)$  are small is disfavoured by data !  
(‘so-called  $B \rightarrow \pi\pi$  puzzle’)
- We also identify model dependence in phenomenological studies due to additional assumptions.
  - **BBNS**  
Identification/parametrization of dominant  $1/m_b$  effects  
(only simple  $1/m_b$  SCET operators considered, not most general parametrization is used)
  - **charming penguins**  
Dominance of certain flavour topologies in naive quark picture  
(relation to QCD/SCET unclear)
  - **$SU(3)$**   
Application of approximate flavour symmetries  
(hadronic errors difficult to estimate)

Standard Isopin Analysis:  $\lambda_i^{(q)} = V_{ib} V_{iq}^*$

$$\sqrt{2} \langle \pi^- \pi^0 | H_{\text{eff}} | B^- \rangle \simeq \lambda_u^{(d)} [3A_u(2, 3/2)] + \lambda_c^{(d)} [3A_c(2, 3/2)] ,$$

$$\langle \pi^+ \pi^- | H_{\text{eff}} | \bar{B}^0 \rangle \simeq \lambda_u^{(d)} [-A_u(0, 1/2) + A_u(2, 3/2)] , \\ + \lambda_c^{(d)} [-A_c(0, 1/2) + A_c(2, 3/2)]$$

$$\sqrt{2} \langle \pi^0 \pi^0 | H_{\text{eff}} | \bar{B}^0 \rangle \simeq \lambda_u^{(d)} [A_u(0, 1/2) + 2A_u(2, 3/2)] \\ + \lambda_c^{(d)} [A_c(0, 1/2) + 2A_c(2, 3/2)] ,$$

$A_i(I, \Delta I)$ :  $I$  denotes the total isospin  $I$  of the final state and  $\Delta I$  the isospin of the operators in the weak effective hamiltonian.

$$A_i(I, \Delta I) = A_i^F(I, \Delta I) + A_i^{NF}(I, \Delta I)$$

- Factorizable Part:

$A_i^F$  fixed by QCD factorization with overall normalization:

$$A_{\pi\pi} = \frac{iG_F}{\sqrt{2}} (m_B^2 - m_\pi^2) F_0^{B \rightarrow \pi}(m_\pi^2) f_\pi$$

- Nonfactorizable Part:

$$A_i^{NF}(I, \Delta I) := r_i(I, \Delta I) e^{i\phi_i(I, \Delta I)} A_{\pi\pi}$$

- \* Unconstrained scenario:

$$0.23 \leq F_0^{B \rightarrow \pi}(m_\pi^2) \leq 0.33 ,$$

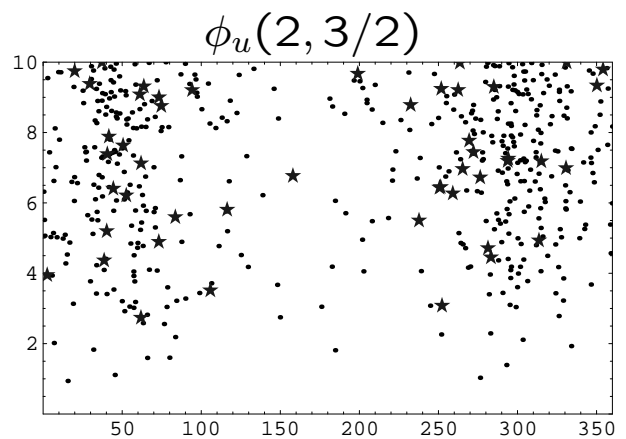
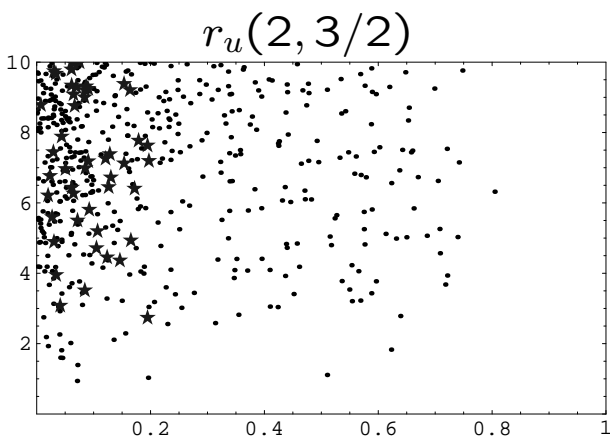
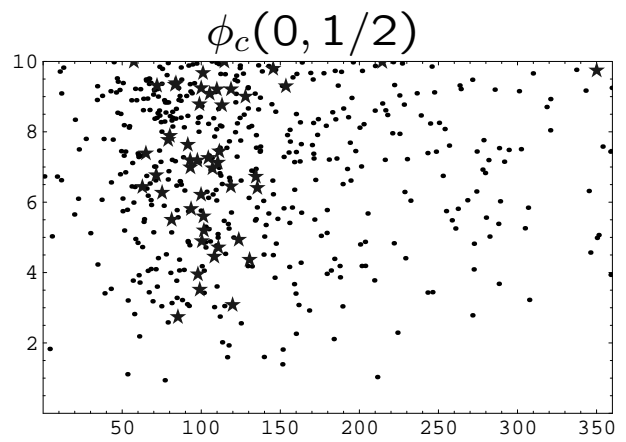
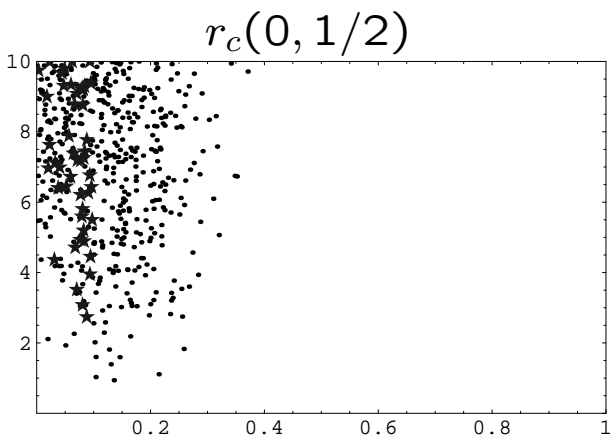
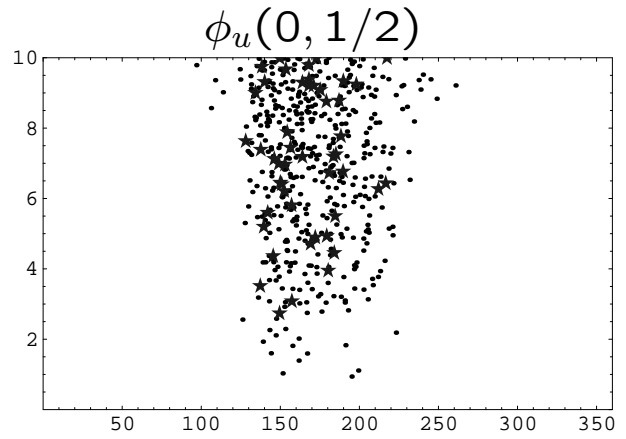
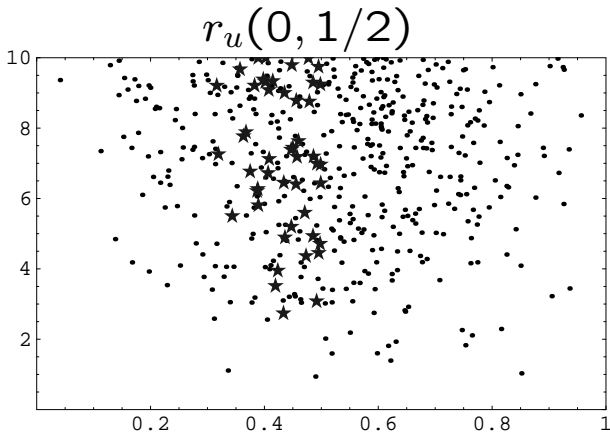
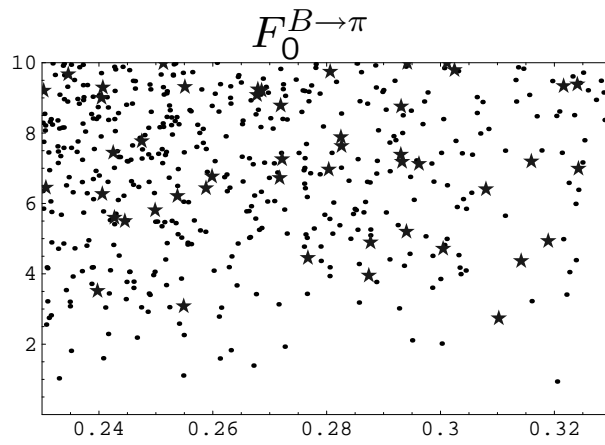
$$0 \leq r_{u,c}(I, \Delta I) \leq 1.0 ,$$

$$0^\circ \leq \phi_{u,c}(I, \Delta I) \leq 360^\circ ,$$

- \* Constrained scenario:

$$r_u(0, 1/2) < 0.5 , \quad r_u(2, 3/2) < 0.2 , \quad r_c(0, 1/2) < 0.1 ,$$

Test also model assumptions of various approaches like dominance of hard-scattering or annihilation terms !



dots for unconstrained,

stars for constrained scenario.

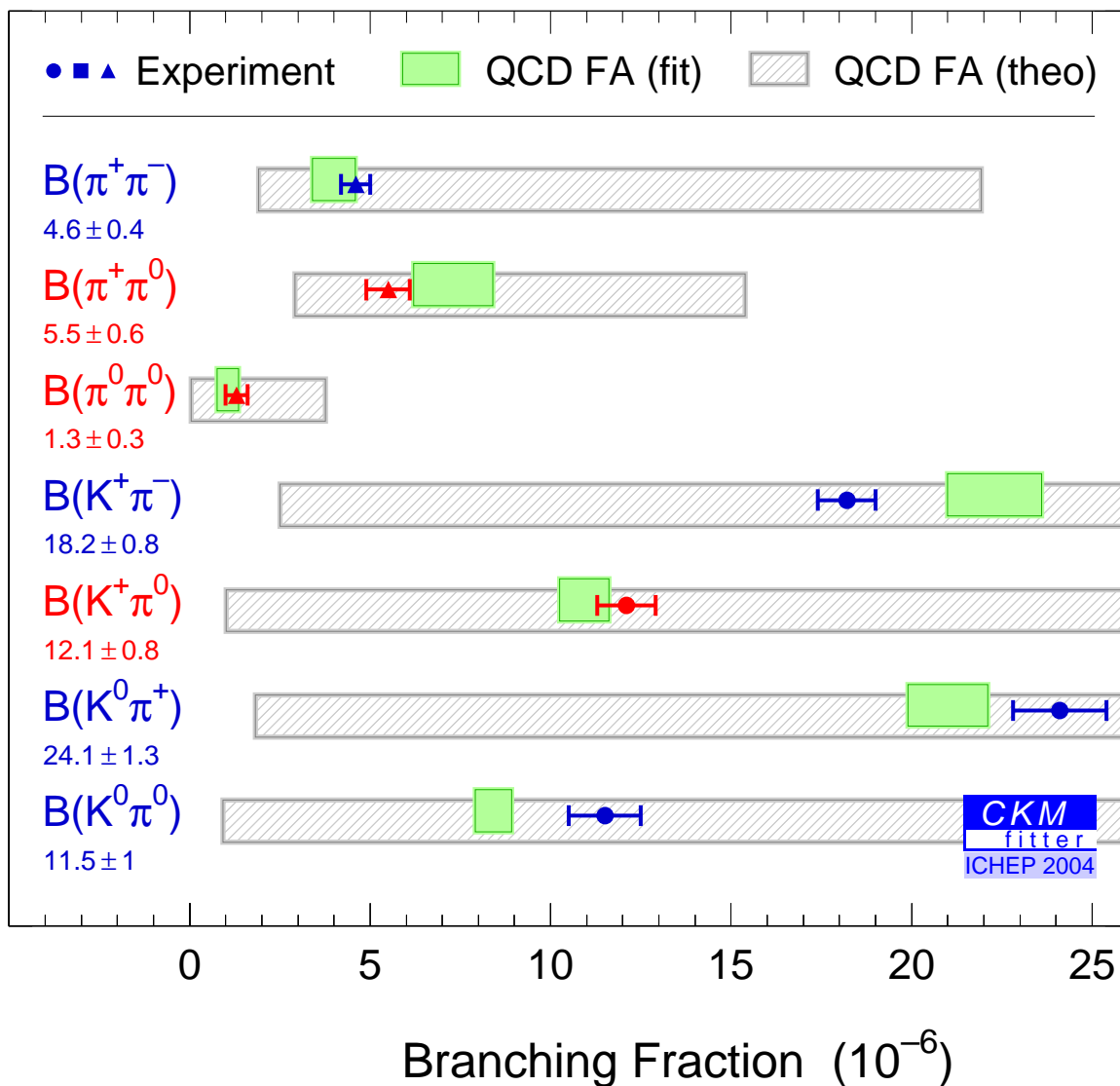
## BBNS versus Experiment

$B \rightarrow \pi\pi$  data not well in line with QCD factorization

\* large modification of some hadronic input parameters ?  
(Beneke, Neubert hep-ph/0308039)

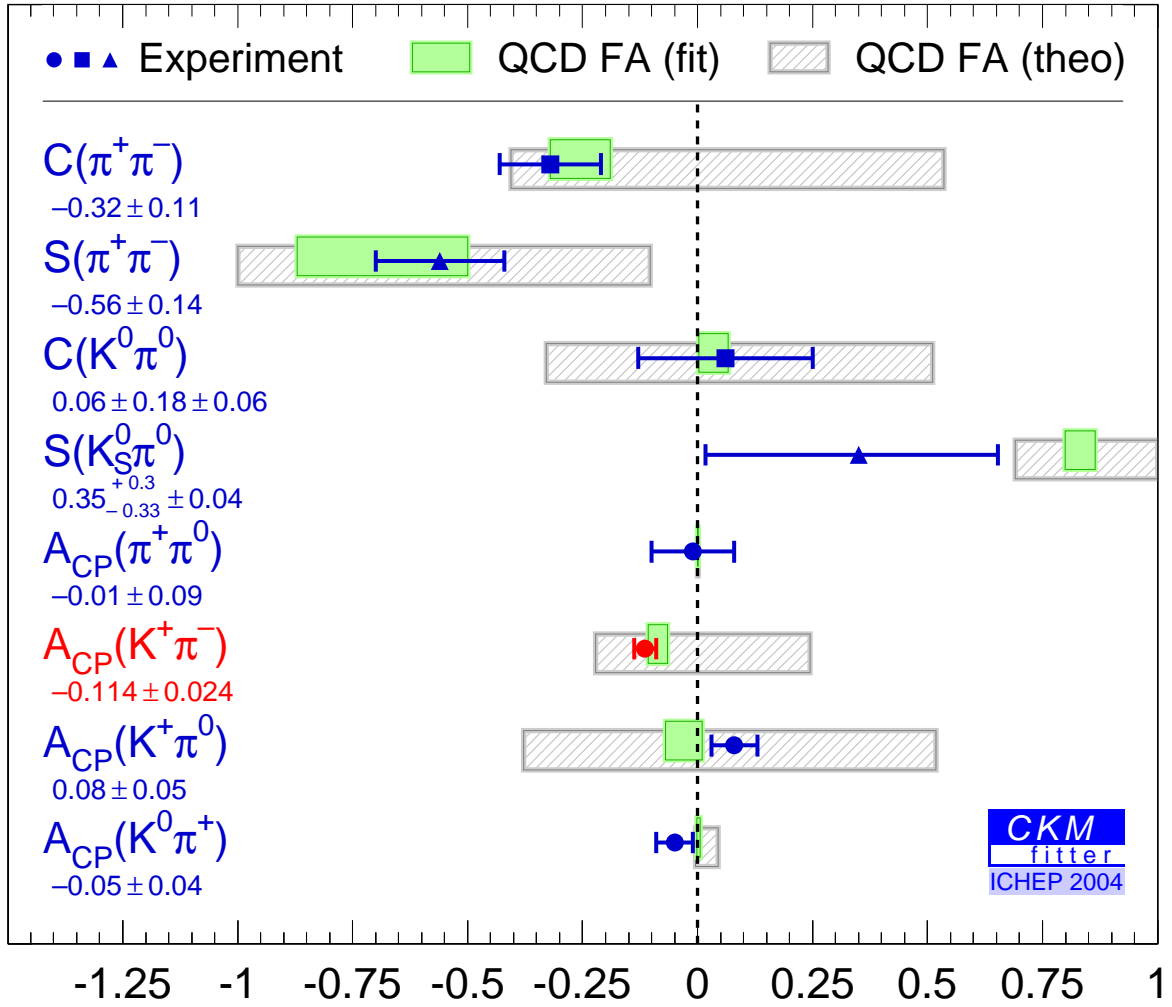
\* safe conclusion: data indicates nonfactorizable contributions are sizable (see scatter plots) !

\* **Fits of BBNS by CKM Fitter group:**  
(the latter fact is not directly manifest in plots)



Fit of theoretical parameters to data

Uncorrelated scan over all theoretical parameters



mixing-induced and direct CP violation

Definitions:

$$A_{CP}[\pi^+\pi^0] = \frac{\Gamma[\bar{B}^- \rightarrow \pi^-\pi^0] - \Gamma[\bar{B}^+ \rightarrow \pi^+\pi^0]}{\Gamma[\bar{B}^- \rightarrow \pi^-\pi^0] + \Gamma[\bar{B}^+ \rightarrow \pi^+\pi^0]},$$

$$S_{\pi\pi}^{+-} = \frac{2\text{Im}\lambda_{\pi\pi}}{1 + |\lambda_{\pi\pi}|^2}, \quad C_{\pi\pi}^{+-} = \frac{1 - |\lambda_{\pi\pi}|^2}{1 + |\lambda_{\pi\pi}|^2},$$

$$\lambda_{\pi\pi} = \frac{q}{p} \frac{\mathcal{A}[\bar{B}^0 \rightarrow \pi^+\pi^-]}{\mathcal{A}[B^0 \rightarrow \pi^+\pi^-]} \simeq e^{-2i\beta} \frac{\mathcal{A}[\bar{B}^0 \rightarrow \pi^+\pi^-]}{\mathcal{A}[B^0 \rightarrow \pi^+\pi^-]}$$

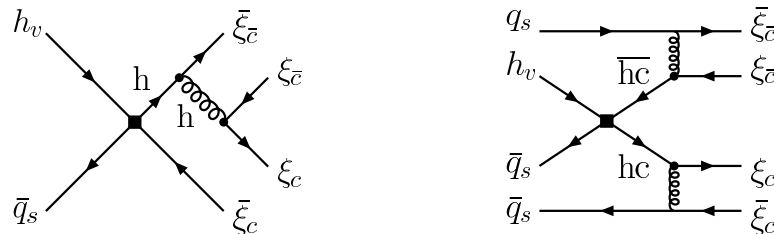


## SCET approach

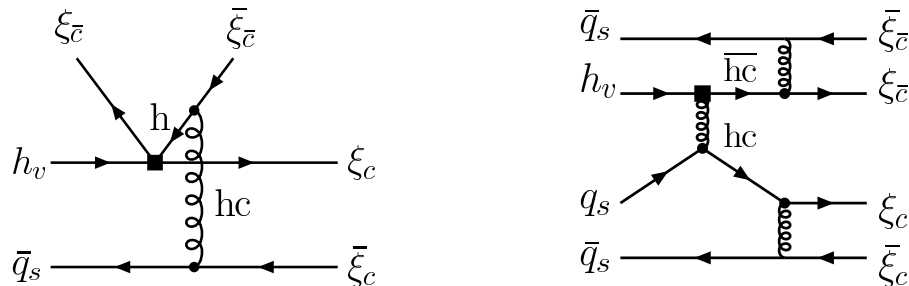
- $1/m_b$  contributions of matrix elements of nonfactorizable SCET operators

For example:

- \* annihilation topologies to  $B \rightarrow PP$



- \* Hard-scattering contributions to  $B \rightarrow PP$



left:

one-gluon exchange included in the BBNS analysis

right:

contributions from higher-Fock-states not necessarily suppressed (nonfactorizable endpoint configurations)

## conclusions on $B \rightarrow \pi\pi$ :

- Use the future data to test various theoretical assumptions on dynamics with the help of a general isospin analysis of the nonfactorizable contributions.
- Challenge for theory:

development of non-perturbative methods within SCET:

SCET sum rules [De Fazio, Feldmann, Hurth hep-ph/0504088](#)

## Is there a $R_n$ -puzzle in $B \rightarrow K\pi$ ?

CP averaged branching ratios:

$$R = \frac{\tau_{B^+} \text{BR}[B_d^0 \rightarrow \pi^- K^+] + \text{BR}[\bar{B}_d^0 \rightarrow \pi^+ K^-]}{\tau_{B^0} \text{BR}[B_d^+ \rightarrow \pi^+ K^0] + \text{BR}[B_d^- \rightarrow \pi^- \bar{K}^0]} = 0.82 \pm 0.056$$

$$R_n = \frac{1}{2} \frac{\text{BR}[B_d^0 \rightarrow \pi^- K^+] + \text{BR}[\bar{B}_d^0 \rightarrow \pi^+ K^-]}{\text{BR}[B_d^0 \rightarrow \pi^0 K^0] + \text{BR}[\bar{B}_d^0 \rightarrow \pi^0 \bar{K}^0]} = 0.789 \pm 0.075$$

$$R_c = 2 \frac{\text{BR}[B_d^+ \rightarrow \pi^0 K^+] + \text{BR}[B_d^- \rightarrow \pi^0 K^-]}{\text{BR}[B_d^+ \rightarrow \pi^+ K^0] + \text{BR}[B_d^- \rightarrow \pi^- \bar{K}^0]} = 1.004 \pm 0.084$$

- pre-ICHEP04 data:

$$R = 0.91 \pm 0.07, \quad R_n = 0.76 \pm 0.10, \quad R_c = 1.17 \pm 0.12$$

- Approach based on QCD factorization (BBNS)

$$R = 0.91^{+0.13}_{-0.11}, \quad R_n = 1.16^{+0.22}_{-0.19}, \quad R_c = 1.15^{+0.19}_{-0.17}$$

- SM-Fit to  $\pi\pi + SU(3)_F$  (Buras et al)

$$R = 0.94^{+0.03}_{-0.03}, \quad R_n = 1.14^{+0.08}_{-0.07}, \quad R_c = 1.11^{+0.06}_{-0.07}$$

(Note: errors reflect only experimental uncertainties of  $B \rightarrow \pi\pi$ )

## Does the $R_n$ puzzle guide us to new physics?

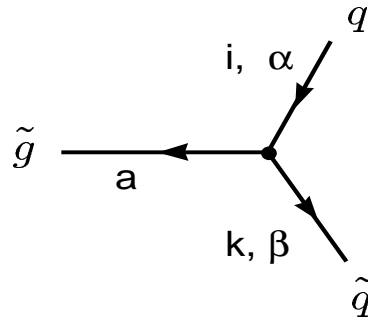
- large nonfactorizable contributions allow for large  $SU(3)_F$  or isospin-violating effects (Feldmann, Hurth)  
(‘so-called  $\pi\pi$  puzzle solves  $K\pi$  puzzle’)
- radiative corrections to decays with charged particles in the final states may not have been taken into account properly in the experimental analysis ( $B^0 \rightarrow \pi^+ K^-$  not yet updated !!)
- possible underestimation of  $\pi_0$  detection efficiency ( $R_n * R_c$ )

## Correlations between $B$ and collider physics via squark mixing within SUSY

- In the unconstrained MSSM there are (too many ?) new contributions to flavour violation
  - CKM induced contributions from  $H^+$ ,  $\chi^+$  exchanges
  - flavour mixing in the sfermion mass matrix

- Gluino-quark-squark coupling

$$-ig_s T_{\beta\alpha}^a (\Gamma_{QL}^{ki} P_L - \Gamma_{QR}^{ki} P_R)$$



- Possible disalignment of quarks and squarks
  - quark mass matrices are diagonal !
  - squarks are rotated 'parallel' to their fermionic superpartners !
  - in general not mass eigenstates:  $\tilde{q}_{L,R} = \Gamma_{QL,R}^+ \tilde{q}_i$

Sfermion mass matrix in uMSSM in  $\tilde{q}_{L,R}$  basis:

$$\mathcal{M}_D^2 = (F/D)_{6 \times 6}^D + \begin{pmatrix} m_{Q,LL}^2 & m_{D,LR}^2 \\ m_{D,RL}^2 & m_{D,RR}^2 \end{pmatrix}$$

$$\mathcal{M}_U^2 = (F/D)_{6 \times 6}^U + \begin{pmatrix} m_{Q,LL}^2 & m_{U,LR}^2 \\ m_{U,RL}^2 & m_{U,RR}^2 \end{pmatrix}$$

from  $F, D$  terms

$3 \times 3$  diagonal submatrices

from soft breaking

$m_i^2$  not diagonal

FCNC are induced by off-diagonal (off-generational) terms in  $m_{LL}^2, m_{RR}^2, m_{LR}^2$

- Low energy constraints

- K-physics:  $\epsilon'/\epsilon$ ,  $K^0$ - $\bar{K}^0$  mixing, ...  
significantly constrain 1 – 2 and 1 – 3 mixing
- B-physics:  $b \rightarrow s\gamma$ ,  $\Delta M_{B_s}$ , ...  
most important beyond SM contributions:  $H^+$ ,  $\tilde{\chi}_i^+$ ,  $\tilde{g}$

- Correlations to Collider Physics (Hurth, Porod)

- squark decays:

$$\begin{aligned}\tilde{u}_i &\rightarrow u_j \tilde{\chi}_k^0, d_j \tilde{\chi}_l^+ \\ \tilde{d}_i &\rightarrow d_j \tilde{\chi}_k^0, u_j \tilde{\chi}_l^-\end{aligned}$$

with  $i = 1, \dots, 6$ ,  $j = 1, 2, 3$ ,  $k = 1, \dots, 4$  and  $l = 1, 2$ .

- these decays are governed by the same mixing matrices as the contributions to flavour violating low-energy observables.

Squarks can have large flavourviolating decay modes (compatible with present data from flavour physics).

## Strategy

- take SPS1a as starting point:

$$M_0 = 100 \text{ GeV}, M_{1/2} = 250 \text{ GeV}$$

$$A_0 = -100 \text{ GeV}, \tan \beta = 10, \mu > 0$$

$\Rightarrow$

$$M_2 = 192 \text{ GeV}, \mu = 351 \text{ GeV}$$

$$m_{H^+} = 403 \text{ GeV}, m_{\tilde{g}} = 594 \text{ GeV}, m_{\tilde{t}_1} = 400 \text{ GeV}$$

$$m_{\tilde{t}_2} = 590 \text{ GeV}, m_{\tilde{q}_R} \simeq 550 \text{ GeV}, m_{\tilde{q}_L} \simeq 570 \text{ GeV}$$

(SPheno 2.0)

- vary off-diagonal squark mass entries.
- accept points with  $2 \leq 10^4 \text{ BR}(b \rightarrow s\gamma) \leq 4.5$  and  $\Delta M_{B_s} \geq 14 \text{ ps}^{-1}$
- For simplicity: real parameters only
- QCD corrections for  $b \rightarrow s\gamma$  as given in [Borzumati et al.](#), Phys. Rev. D62, 075005 (2000) and [Besmer et al.](#), Nucl.Phys.B609:359 (2001)
- $\Delta M_{B_s}$ , as given in [Baek et al.](#), Phys. Rev. D64, 095001 (2001)

$\Rightarrow$  Typical results:

Branching ratios (in %) of  $u$ -type squarks

	$\tilde{\chi}_1^0 c$	$\tilde{\chi}_1^0 t$	$\tilde{\chi}_2^0 c$	$\tilde{\chi}_2^0 t$	$\tilde{\chi}_3^0 c$	$\tilde{\chi}_3^0 t$	$\tilde{\chi}_4^0 c$	$\tilde{\chi}_4^0 t$	$\tilde{\chi}_1^+ s$	$\tilde{\chi}_1^+ b$	$\tilde{\chi}_2^+ s$	$\tilde{\chi}_2^+ b$
$\tilde{u}_1$	4.7	18	5.2	9.6	$6 \times 10^{-3}$	0	0.02	0	11.3	46.4	$2 \times 10^{-3}$	4.7
$\tilde{u}_2$	19.6	1.1	0.4	17.5	$2 \times 10^{-2}$	0	$6 \times 10^{-2}$	0	0.5	57.5	$3 \times 10^{-3}$	2.9
$\tilde{u}_3$	7.3	3.7	20	1.4	$6 \times 10^{-2}$	0	0.6	0	40.3	3.1	1	18.5
$\tilde{u}_6$	5.7	0.4	11.1	5.3	$4 \times 10^{-2}$	5.7	0.6	13.2	22.9	13.1	0.6	8.0

Branching ratios (in %) of  $d$ -type squarks

	$\tilde{\chi}_1^0 s$	$\tilde{\chi}_1^0 b$	$\tilde{\chi}_2^0 s$	$\tilde{\chi}_2^0 b$	$\tilde{\chi}_3^0 s$	$\tilde{\chi}_3^0 b$	$\tilde{\chi}_4^0 s$	$\tilde{\chi}_4^0 b$	$\tilde{\chi}_1^- b$	$\tilde{\chi}_1^- t$	$\tilde{\chi}_2^- b$	$\tilde{\chi}_2^- t$	$\tilde{u}_1 W^-$
$\tilde{d}_1$	1.2	5.7	8.4	30.6	$2 \times 10^{-2}$	1.5	0.2	0.9	16.6	34.1	0.6	0	0
$\tilde{d}_2$	17.4	5.8	5.1	15.7	$7 \times 10^{-2}$	7.4	0.3	09.2	9.7	19.7	0.7	0	8.8
$\tilde{d}_4$	14.7	21.7	11.3	2.2	$5 \times 10^{-2}$	10.6	0.5	8.4	22.1	3.6	1.2	0	3.4
$\tilde{d}_6$	1.7	0.5	20.5	6.9	0.1	0.9	1.2	1.3	40.3	10.2	3.4	11.1	1.8

Glauino branching ratios larger than 1%.

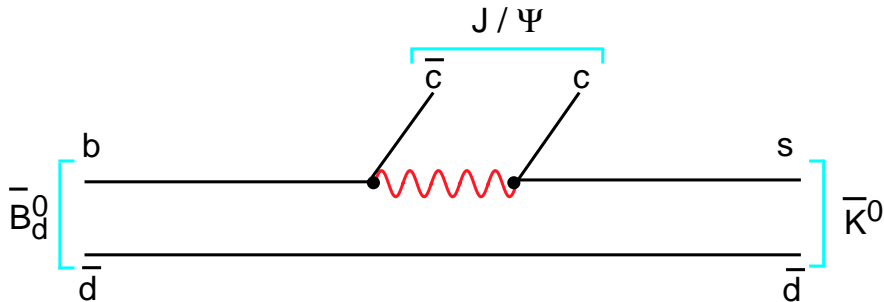
Final state	BR [%]	Final state	BR [%]
$\tilde{u}_1 c$	12.9	$\tilde{d}_1 s$	7.2
$\tilde{u}_1 t$	5.7	$\tilde{d}_1 b$	19.8
$\tilde{u}_2 c$	0.4	$\tilde{d}_2 s$	6.1
$\tilde{u}_2 t$	7.6	$\tilde{d}_2 b$	4.7
$\tilde{u}_3 c$	0.6	$\tilde{d}_3 d$	10.0
$\tilde{u}_4 u$	5.5	$\tilde{d}_4 s$	3.5
$\tilde{u}_5 u$	3.0	$\tilde{d}_4 b$	4.9
		$\tilde{d}_5 d$	2.1

### conclusions on correlations via squark mixing

- $b \rightarrow s\gamma$  and  $\Delta M_{B_s}$  (still ?) allow for large mixings between second and third generation squarks, for example  $\tilde{t}_i, \tilde{c}_i$  can have large flavour violating decay modes,
- makes life at LHC potentially more interesting and more difficult,
- extra information from ILC or flavour factories needed.

## CP Violating Observables

- SM is very predictive **only one CP-violating parameter**. (Kobayashi-Maskawa 1972 !)
- **KM mechanism has passed successfully its first precision test:**



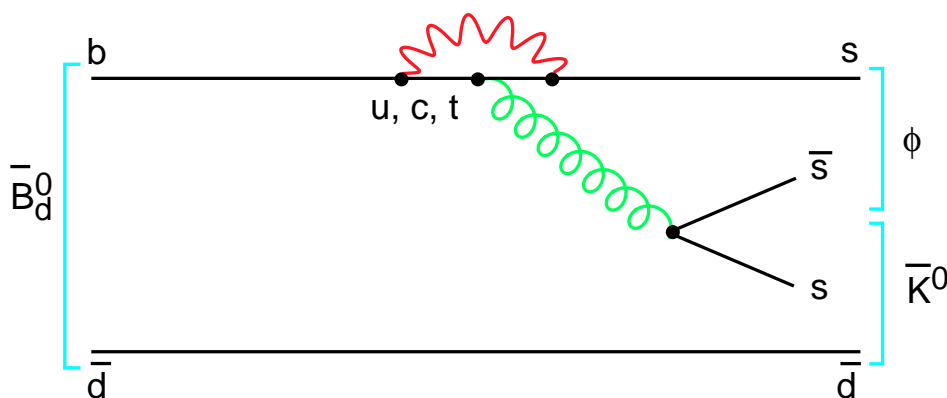
$$A_{CP}(t) = \frac{\Gamma(\bar{B}^0(t) \rightarrow f) - \Gamma(B^0(t) \rightarrow f)}{\Gamma(\bar{B}^0(t) \rightarrow f) + \Gamma(B^0(t) \rightarrow f)}$$

$$A_{CP}(B_d \rightarrow J/\psi K_S) = \sin(2\beta) \sin(\Delta m_{BT}) \quad \Delta B = 2$$

$$\sin(2\beta) = \begin{cases} 0.741 \pm 0.067 \pm 0.033 & \text{Babar} \\ 0.733 \pm 0.057 \pm 0.028 & \text{Belle} \end{cases}$$

$$\text{SM: } \sin(2\beta) = 0.68 \pm 0.21$$

- **Test in  $A_{CP}(B_d \rightarrow \Phi K_S)$  is still open: Penguin**



- **Also direct CP asymmetries in  $b \rightarrow s/d$  transitions:  $\Delta F = 1$ :**

$$\Delta\Gamma_{CP}(B \rightarrow X_{s/d}\gamma) = \Gamma(\bar{B} \rightarrow X_{s/d}\gamma) - \Gamma(B \rightarrow X_{\bar{s}/\bar{d}}\gamma)$$

$$|\Delta BR_{CP}(B \rightarrow X_s\gamma) + \Delta BR_{CP}(B \rightarrow X_d\gamma)| \sim 1 \cdot 10^{-9} \approx 0$$

(Hurth, Mannel)



Untagged CP asymmetries in  $b \rightarrow s/d$  transitions  $\Delta F = 1$

$$\Delta\Gamma_{CP}(B \rightarrow X_{s/d}\gamma) = \Gamma(\bar{B} \rightarrow X_{s/d}\gamma) - \Gamma(B \rightarrow X_{\bar{s}/\bar{d}}\gamma)$$

KM mechanism CKM unitarity

$$\Rightarrow J = \text{Im}(\lambda_u^{(s)}\lambda_c^{(s)*}) = (-1) \text{Im}(\lambda_u^{(d)}\lambda_c^{(d)*})$$

+ U spin symmetry of matrix elements  $d \leftrightarrow s$ :

$$\Delta\Gamma_{CP}(B \rightarrow X_s\gamma) + \Delta\Gamma_{CP}(B \rightarrow X_d\gamma) = b_{inc}\Delta_{inc}$$

$b_{exc}$ : 'relative U-spin-breaking';  $|b_{inc}| \sim m_s^2/m_b^2 \sim 5 \cdot 10^{-4}$

$\Delta_{exc}$ : 'typical size' of CP violating rate difference

$$|\Delta BR_{CP}(B \rightarrow X_s\gamma) + \Delta BR_{CP}(B \rightarrow X_d\gamma)| \sim 1 \cdot 10^{-9} \approx 0$$

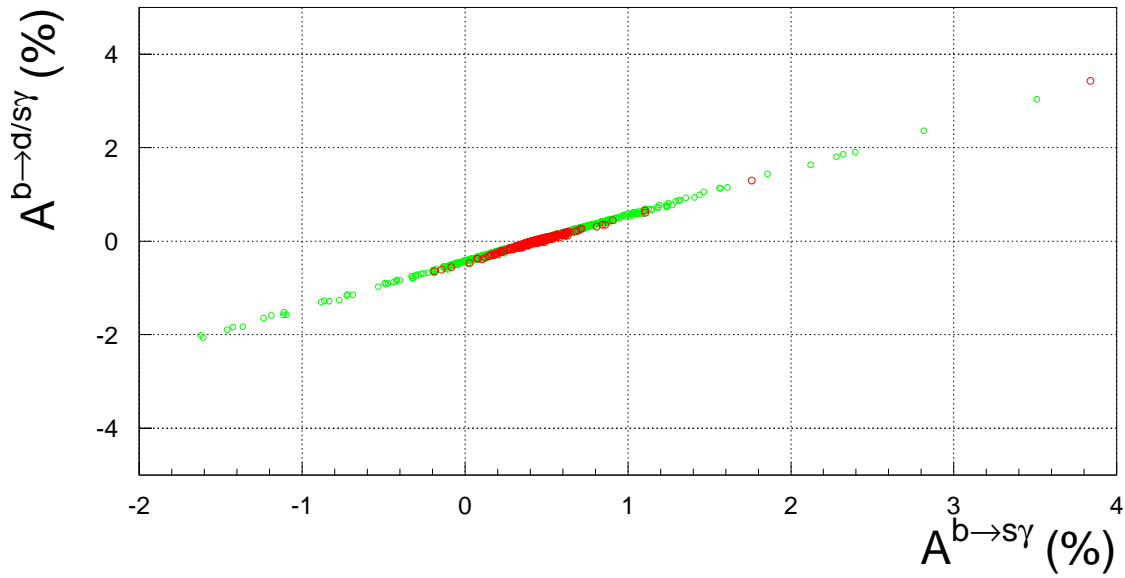
Clean test, whether new CP phases are active or not  
(Hurth, Mannel)

Experiment: (Super-) Babar  $\pm 3\%$  ( $\pm 0.3\%$ ) precision possible

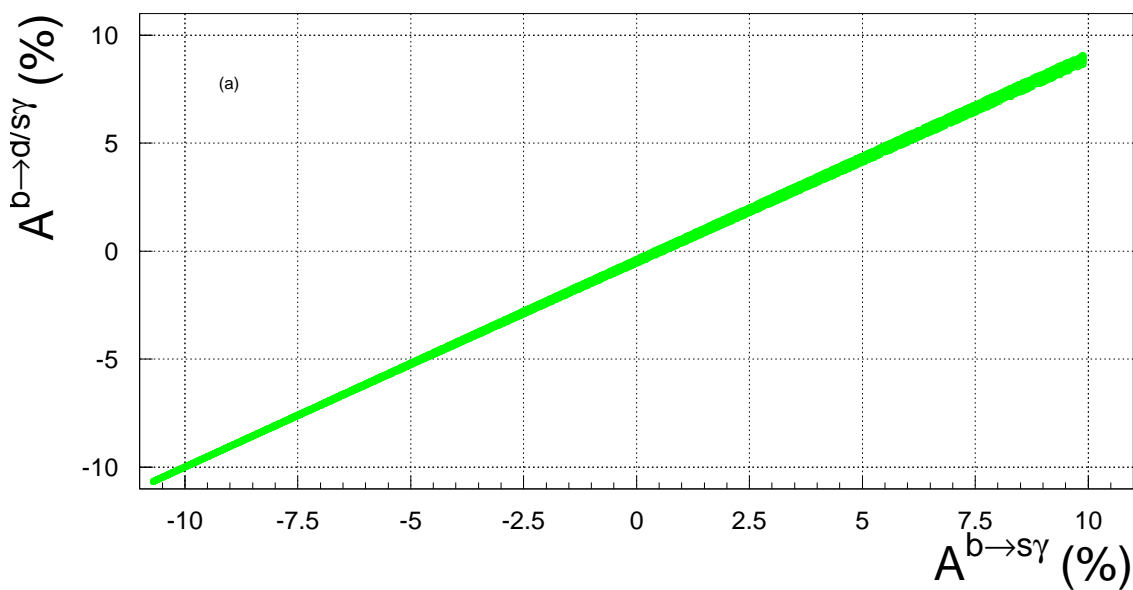
$$A_{CP}(b \rightarrow (s + d) \gamma) = \frac{A_{CP}^{b \rightarrow s\gamma} + R_{ds} A_{CP}^{b \rightarrow d\gamma}}{1 + R_{ds}}, \quad R_{ds} = \Sigma \Gamma_d / \Sigma \Gamma_s$$

Experiment: Babar  $\pm 3\%$  (Super-Babar  $\pm 0.3\%$ ) uncertainty

MFV with (flavourblind) phases



Model-independent analysis  $C_7^s$ ; squark mixing  $\delta_{23}$ :



(Hurth, Lunghi, Porod)

## Experimental Issues

- Inclusive **untagged** measurement with other-side-lepton tag
  - efficiencies on  $A_{CP}^{b \rightarrow s \gamma}$  and on  $A_{CP}^{b \rightarrow d \gamma}$  the same
  - advantage of a high photon energy cut at  $2.2 \text{ GeV}$  can be used
  - present  $81 \text{ fb}^{-1}$  data set leads to an estimated 11% precision, dominated by statistical error **Libby, Babar**
  - Extrapolation **Libby, Babar**

$1 \text{ ab}^{-1}$	3%	end of Babar/Belle
$10 \text{ ab}^{-1}$	1%	one-year running SuperBabar
$50 \text{ ab}^{-1}$	0.3%	end of SuperBabar
- Planned: Inclusive **tagged** measurement
  - independent data sample with an additional kaon tag
  - smaller mistag fraction
- Semi-inclusive measurement
  - not clear if quark-hadron duality applicable if only 50% of the rate available

## conclusions on direct CP

- Untagged CP asymmetry favoured observable, perhaps even more information, cleaner than tagged  $A_{CP}$
- Discrimination power between various scenarios
- Restricted indirect sensitivity for  $A_{CP}^{b \rightarrow d \gamma}$  through tagged + untagged  $A_{CP}$

# FLAVOUR IN THE ERA OF THE LHC

a Workshop

on the interplay of flavour and collider physics

First meeting: CERN, November 7-11 2005

<http://mlm.home.cern.ch/mlm/FlavLHC.html>

The goal of this Workshop is to outline and document a programme for flavour physics for the next decade, addressing in particular the complementarity and synergy between the LHC and the flavour factories vis a vis the discovery and exploration potential for new physics.

The format of the Workshop will follow the standard CERN experience, with an opening meeting with plenary sessions and with the start of the WG activities, followed by 2-3 meetings of the WG's to take place during the following year, and a final plenary meeting at the end.